Chinese Character Font Recognition using Fourier Spectrum Features and Back-propagation Neural Network*

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Abstract

A simple and feasible approach to Chinese character font recognition using Fourier spectrum features and the back-propagation neural network is proposed. An input image with one Chinese character bitmap pattern is transformed into the frequency domain using the Fourier transform. The Fourier amplitude spectra of the transformed image is then divided into non-overlapping square blocks with nonequal sizes, and a spectrum feature vector is derived from the mean amplitudes of the square blocks. A back-propagation neural network classifier is used to recognize the font types of Chinese characters after learning. Experiments have been conducted in which training samples and test samples were selected randomly from 5,401 most frequently used Chinese characters. An average recognition rate of 86% for font recognition of a single character and average recognition rates of 96%-100% for font recognition of a string with an identical font were obtained for the six most popular fonts, which shows the feasibility and efficiency of the proposed approach for Chinese character font recognition. The method can be used in character recognition and document analysis applications.

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1. Introduction

Huge amounts of printed materials, such as newspapers, journals, magazines, and office documents are published every day. Various document components, such as headlines, text lines, and graphics, are used to distinguish articles and indicate article contents. To more effectively access the information contained within such documents, an automated document entry system is needed to handle different layout styles[1]. Various techniques, such as document image segmentation, character segmentation, and character recognition have been investigated for use in an automated document entry system, but font recognition is seldom considered.

Artificial neural network techniques have recently been applied to many different fields and have demonstrated capabilities in solving complex problems. The error back-propagation method proposed by Rumelhart[2,3] is a representative learning method for hierarchical networks. Hirose et al.[4] proposed a back-propagation algorithm that varies the number of hidden units which can be used to escape local minima and make it unnecessary to decide the number of hidden units. In this study, we use the back-propagation neural network model as a classifier to recognize the Chinese character font because of the high capability of learning and the high speed of recalling of the model.

The Chinese character font recognition problem is more diffucult than that of English because the size of the Chinese character set is larger and the strokes of the Chinese characters are more complicated. Morris[5] used spectral signatures[6] and a statistical analysis method[7] to recognize the English digital typefaces. The samples used in [5] consist of strings selected at random from English text. Each string is rendered in a particular typeface and truncated to an image of 512x64 pixels. Then a 512x64

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discrete Fourier transform of the string is computed and the amplitudes at each of the resulting points recorded. In the classification stage using ideal filters, the spatial frequency plane is first partitioned into 38 rectangular regions, and the mean Fourier amplitude of each region is computed and collected as a feature vector. By assuming that the class conditional densities are normal, a piecewise quadratic classifier was used as an approximation to the Bayes minimum error classifier. Jou et al.[8] proposed universal data compression a algorithm to model chinese character patterns and a scheme based on the universal model for recognizing the Chinese character font. They used 10,000 Chinese characters with the same font as an input source sequence to obtain the universal model. After different models were built, a long string of input characters were simultaneously encoded using different models obtained from different character fonts. The character font type is finally decided to be the model that yields the largest compression ratio. In this study, we use features extracted from certain bands of the Fourier amplitude spectrum of each character image as the input of the classifier. An average recognition rate of 86% for font recognition of a single character and average recognition rates of 96%-100% for font recognition of a string with an identical font using an average technique can be obtained for the six most popular fonts. Experimantal results show the feasibility and efficiency of the proposed approach for Chinese character font recognition. It can be used in character recognition and document analysis applications.

The remainder of this paper is organized as follows. A brief review of the Fourier transform and the back-propagation neural network is given in Section 2. In Section 3, the proposed Chinese character font recognition method is presented. Several experimental results showing the feasibility of the proposed approach are described in Section 4. Finally, some conclusions are given in Section 5.

2. Review of Fourier Transform and Back-propagation Neural Network

2.1 Fourier Transform

A 2D image i may be reguarded as a real-valued function on the plane, where i(x, y) denotes the image intensity at (x, y). The

Fourier transform $I(\omega_x, \omega_y)$ of i(x, y) is given by

$$I(\omega_x, \omega_y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} i(x, y) e^{-j2\pi(x\omega_x + y\omega_y)} dxdy.$$
 (1)
It can be written in polar coordinates as

$$I(\omega_x, \omega_y) = A(\omega_x, \omega_y)e^{i\phi(\omega_x, \omega_y)},$$
 (2)
where $A(\omega_x, \omega_y) = |I(\omega_x, \omega_y)|$ is the
Fourier amplitude at (ω_x, ω_y) and $\phi(\omega_x, \omega_y)$ the Fourier phase at (ω_x, ω_y) .

The variables ω_r and ω_v denote the spatial frequencies and roughly represent the rate at which the image is changing in its intensity in the x and y directions, respectively. High spatial frequencies correspond to rapid rates of changes with respect to position, i.e., correspond to small features in the image. On the other hand, low spatial frequencies correspond to slow rates of changes, i.e., correspond to large features. The amplitude denotes the amount of variation at the given spatial frequency. Large amplitudes at a given spatial frequency or block of frequencies accompany prominent features repeating at those frequencies. Thus, the amplitude encodes the amount of variation in features. The phase, on the other hand, encodes the gross position of The differences of the Chinese features. character fonts come from the sizes of the characters, the thicknesses of the strokes, and the slopes of the characters, etc. For these reasons, it is natural to expect that the amplitude distribution of the frequency plane might have font-specific information. The Chinese character fonts do not depend on the positions of the strokes. Thus, we may ignore the effect of phases.

2.2 Back-Propagation Neural Network

Back propagation is often used as the learning algorithm in layered-structure neural networks because of its efficiency. The algorithm is a learning rule which suggests a way of modifying weights to represent a function from input to output. The network architecture incldes an input layer, one or more hidden layer(s), and an output layer. The units on a layer have full connections to the units on the adjacent layers, but no connection to the units on the same layer, as shown in Figure 1. A way of

computing the function from the input to the output is to calculate the difference (or the error) between the expected and actual output value and to adjust the weights in order to minimize the error. The algorithm minimizes the error by performing a gradient descent on the error surface in the weight space whose height at any point in the weight space is equal to the error measure. Thus, the amount of the weight change for each input pattern in a learning cycle is proportional to the error; a learning cycle is completed after the network sees all of the input and output pairs. The error is gradually reduced to a certain point as the number of learning cycles is increased. In the case of the threelayered back-propagation neural network model shown in Figure 1, the algorithm assigns the input vector as an output vector of the input layer; no transformation occurs in the input layer. The output vector of the input layer propagates forward to the hidden units to compute the output values of the hidden units, H, with the help of a sigmoid output function defined as follows:

$$H_{k} = 1 / \left\{ 1 + \exp \left[-\sum_{i=0}^{n} W_{ki} X_{i} - \theta_{k} \right] \right\}$$
 (3)

where X_i is the output value of the *i*th unit in the input layer, θ_k is a threshold of the *k*th unit in the hidden layer, W_{ki} is the connection weight between the *i*th unit in the input layer, and the *k*th unit in the hidden layer. The output vector of the hidden layer then propagates forward to the output unit to calculate the output value of the final output layer, O, by the same output function using U_{jk} and H_k instead defined as follows:

$$O_{j} = 1 / \left\{ 1 + \exp \left[-\sum_{k=0}^{n} U_{jk} H_{k} - \theta_{j} \right] \right\}$$
 (4)

where θ_j is a threshold of the jth unit in the output layer, U_{jk} is the connection weight between the kth unit in the hidden layer, and the jth unit in the output layer. The output value from the output layer is compared with the desired one to compute a sum of squared errors according to

$$E = \frac{1}{2} \sum_{j=0}^{n} (D_{j} - O_{j})^{2}, \qquad (5)$$

where D_j is the desired and O_j is the actual output values of the final output layer computed

by (4). The connection weight between the jth unit in the output layer and the kth unit in the hidden layer is modified according to

$$\Delta U_{jk} = \eta \delta_j H_k , \qquad (6)$$

where

$$\boldsymbol{\delta}_{j} = \left(D_{j} - O_{j}\right) O_{j} \left(1 - O_{j}\right) . \tag{7}$$

The connection weight between the kth unit in the hidden layer and the ith unit in the input layer is modified according to

$$\Delta W_{ki} = \eta \delta_k X_i , \qquad (8)$$

where

$$\delta_k = H_k (1 - H_k) \sum_{i=0}^n \delta_i U_{jk} . \qquad (9)$$

The value η in (6) and (8) is a scalar quantity which determintes the rate of the gradient descent. In training a network, a small value of η leads to slower learning; however, a large value of η may lead to a local minimum. A moderate value smaller than 1.0 is often found appropriate for η . The learning process is repeated for a number of times until the change of weights become negligible.

3. Proposed Approach to Chinese Character Font Recognition

A Chinese character may be seen as a 2dimensional pattern with a number of strokes. Each stroke consists of a cluster of black points, and the area outside the strokes is filled with white points. Each character pattern stands for an individual meaning, unlike English words which are spelled in a string of letters from the 26-letter Roman alphabet. We select six types of most popular Chinese fonts for use in this study. Some examples are shown in Figure 2. A scanned document image like the one shown in Figure 3 is first thresholded to a bitmap image. Isolated character patterns with 64x64 in size obtained after a segmentation and normalization process is performed. The result of such a process of Figure 3 is shown in Figure 4. We use the resulting character samples for learning and testing later. Two methods for font recognition are proposed in this study and are described in the following.

3.1 An integrated method

In general, there are two steps in pattern recognition. The first is the feature extraction step and the other is the classification step. We use the Fourier transform for feature extraction and the back-propogation neural network for classification. A character sample is first transformed into the spatial frequency plane by a 64x64 discrete Fourier transform. The amplitude at each of the resulting points is recorded. Some results were shown in Figure 5, Figure 6, and Figure 7. We can see that the most different amplitudes in those figures are located on the low frequency areas. Then, the spatial frequency plane is divided into 50 non-overlapping square blocks with varying sizes as shown in Figure 8. The mean Fourier amplitude of each square block is computed. Finally we take these mean values to form a feature vector for use in the classification step.

As to the structure of the back-propagation neural network model, we use 50 units in the input layer for the 50-dimensional feature vector, 25 units in the hidden layer, and 6 units in the output layer for the six font types.

3.2 An average technique

In general, font recognition of a string with an identical font is more practical than font recognition of a character only. In this study we also use the technique for single character font recognition described previously to recognize string font recognition by an average principle. The proposed method is to compute, for a given string of characters all with a single font, the following measure, called the Fourier amplitude of the string at (ω_x, ω_y) ,

$$\overline{A}(\omega_x, \omega_y) = \sum_{i=1}^n A_i(\omega_x, \omega_y) / n, \qquad (10)$$

where n is the length of the string, and $A_i(\omega_x, \omega_y)$ is the Fourier amplitude of the ith character in the string. This method enhances the common property of different characters with a single font by the way of summation, but decreases the effect coming from different characters by the way of averaging. We can also use the technique to recognize the font type of a Chinese text block with some characters which is rendered in an identical font by the way of selecting n characters in the block at random.

4. Experimental Results

The proposed methods have been tested using a personal computer. Figure 9 shows some training characters which are selected randomly from the 5,401 most-frequently used characters. Figure 10 shows a tested document with six blocks. There are 50 characters with a single font in each block. Each block has a distinct font type.

For font recognition of a single character using the integrated method, we made three experiments which are different in the numbers of used training characters. 33 characters were used for training in the first experiment, 100 characters in the second, and 300 characters in the last. The confusion tables of the above three experiments are shown in Table 1, Table 2, and Table 3, respectively. The leftmost columns of Figure 11, Figure 12, and Figure 13 show respectively the classification results of the above three experiments, in which the tested characters are selected sequentially from the tested document with the six blocks shown in Figure 10. The overall correct classification rates of the three experiments are shown in Table 4. We can see that a higher recognition rate comes from the use of a larger number of training characters.

For font recognition of a string with an identical font using the average technique, we use the same classifiers used in font recognition of a single character and we made three experiments which are different in the lengths of tested strings. The tested strings are selected sequentially from the tested document shown in Figure 10. Strings consisting of two characters were tested in the first experiment, five characters in the second, and ten characters in the last. The confusion tables of the first experiment using the three classifiers(i.e., classifiers trained with 33,100, and 300 characters) which were obtained in experiments for font recognition of single characters are shown in Table 5, Table 6, and Table 7, respectively. The confusion tables of the second experiment using the three classifiers are shown in Table 8, Table 9, and Table 10, respectively. The confusion tables of the last experiment using the three classifiers are shown in Table 11, Table 12, and Table 13, respectively. The rightmost three columns of Figure 11, Figure 12, and Figure 13 show respectively the classification results of the above three experiments. The overall correct classification rates of the three experiments are shown in Table 14. We can see that a higher recognition rate comes from the use of a larger number of training characters and a larger length of the tested string with the same font.

5. Conclusion

A feasible approach to the Chinese font recognition has been proposed. The approach is based on the use of Fourier spectrum features and the back-propagation neural network. Some important results were obtained in this study. First, high recognition rates have been obtained in our experiments. Second, the number of training characters is much smaller than 10,000 which is needed in [8]. Third, we can use the method not only for font recognition of a single character but also for font recognition of a string with identical fonts. The last, the approach is simple and effective. It can be improved by increasing the number of training characters, or by dividing the spatial frequency plane more properly. The font recognition result can be used in Chinese character recognition and document analysis applications.

References

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Table 1. Confusion table of the first experiment.

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	43	0	5	1	1	0
font 2	0	36	0	0	11	3
font 3	5	0	35	6	0	4
font 4	8	0	0	42	0	0
font 5	0	8	2	0	37	3
font 6	6	1	3	0	1	45

Table 2. Confusion table of the second experiment

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	45	0	3	1	1	0
font 2	0	45	0	0	1	4
font 3	6	0	38	5	0	1
font 4	7	0	2	39	0	2
font 5	0	1	2	0	43	4
font 6	2	2	4	1	0	41

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Table 3. Confusion table of the third experiment.

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	40	0	9	0	1	0
font 2	0	47	0	0	1	2
font 3	3	0	42	1	0	4
font 4	1	0	6	42	0	1
font 5	0	5	0	0	42	3
font 6	0	2	2	0	2	44

Table 4. The recognition rates for different numbers of training characters in six Chinese fonts.

experi	The	Learni	recog.	recog.	
ment	number of	ng	rates for	rates for	
	training	Cycles	Training	Tested	
	characters		characters	characters	
1	33	95	99%	79%	
2	100	254	96%	84%	
3	300	711	96%	86%	

Table 5. Confusion table of the first experiment using the average technique by the classsifier which was obtained in the first experiment using the integrated method (the lengths of test strings are two).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	24	0	1	0	0	0
font 2	0	20	0	0	3	2
font 3	4	0	19	2	0	0
font 4	4	0	0	21	0	0
font 5	0	2	0	0	23	0
font 6	0	0	2	0	0	23

Table 6. Confusion table of the first experiment using the average technique by the classifier which was obtained in the second experiment using the integrated method (the lengths of test strings are two).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	25	0	0	0	0	0
font 2	0	23	0	0	0	2
font 3	3	0	20	2	0	0
font 4	2	0	1	22	0	0
font 5	0	0	0	0	25	0
font 6	0	0	2	0	0	23

Table 7. Confusion table of the first experiment using the average technique by the classifier which was obtained in the last experiment using the integrated method (the lengths of test strings are two).

	font 1	font 2	font 3	font 4	font 5	font 6
font l	23	0	2	0	0	0
font 2	0	24	0	0	0	1
font 3	0	0	25	0	0	0
font 4	0	0	1	24	0	0
font 5	0	1	0	0	24	0
font 6	0	1	0	0	0	24

Table 8. Confusion table of the second experiment using the average technique by the classifier which was obtained in the first experiment using the integrated method (the lengths of test strings are five).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	10	0	0	0	0	0
font 2	0	10	0	0	0	0
font 3	1	0	9	0	0	0
font 4	0	0	0	10	0	0
font 5	0	0	0	0	10	0
font 6	0	0	0	0	0	10

Table 9. Confusion table of the second experiment using the average technique by the classifier which was obtained in the second experiment using the integrated method (the lengths of test strings are five).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	10	0	0	0	0	0
font 2	0	9	0	0	0	1
font 3	1	0	9	0	0	0
font 4	0	0	0	10	0	0
font 5	0	0	0	0	10	0
font 6	0	0	0	0	0	10

Table 10. Confusion table of the second experiment using the average technique by the classifier which was obtained in the last experiment using the integrated method (the lengths of test strings are five).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	10	0	0	0	0	0
font 2	0	10	0	0	0	0
font 3	0	0	10	0	0	0
font 4	0	0	0	10	0	0
font 5	0	0	0	0	10	0
font 6	0	0	0	0	0	10

Table 11. Confusion table of the last experiment using the average technique by the classifier which was obtained in the first experiment using the integrated method (the lengths of test strings are ten).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	5	0	0	0	0	0
font 2	0	5	0	0	0	0
font 3	0	0	5	0	0	0
font 4	0	0	0	5	0	0
font 5	0	0	0	0	5	0
font 6	0	0	0	0	0	5

Table 12. Confusion table of the last experiment using the average technique by the classifier which was obtained in the second experiment using the integrated method (the lengths of test strings are ten).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	5	0	0	0	0	0
font 2	0	5	0	0	0	0
font 3	0	0	5	0	0	0
font 4	0	0	0	5	0	0
font 5	0	0	0	0	5	0
font 6	0	0	0	0	0	5

Table 13. Confusion table of the last experiment using the average technique by the classsifier which was obtained in the last experiment using the integrated method (the lengths of test strings are ten).

	font 1	font 2	font 3	font 4	font 5	font 6
font 1	5	0	0	0	0	0
font 2	0	5	0	0	0	0
font 3	0	0	5	0	0	0
font 4	0	0	0	5	0	0
font 5	0	0	0	0	5	0
font 6	0	0	0	0	0	5

Table 14. The recognition rates for different numbers of training characters in six Chinese fonts.

_	The length of tested strings						
The number of training characters	2	5	10				
33	87%	98%	100%				
100	92%	97%	100%				
300	96%	100%	100%				

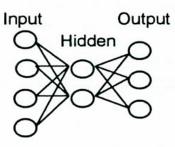


Figure 1. A three-layered neural network model.

交通大學	(font type 1)
交通大學	(font type 2)
交通大學	(font type 3)
交通大學	(font type 4)
交通大學	(font type 5)
交通大學	(font type 6)

Figure 2. Example of Chinese font types.

Figure 3. Part of a scanned character image.

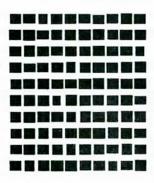


Figure 4. Segmentation results of the image shown in Figure 3.

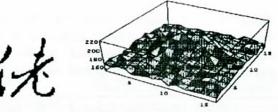


Figure 5. An isolated character pattern of font type 1 and its Fourier transform plane.

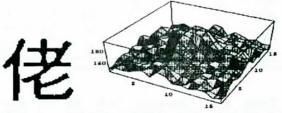


Figure 6. An isolated character pattern of font type 2 and its Fourier transform plane.

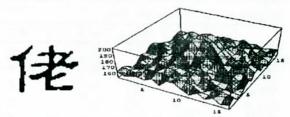


Figure 7. An isolated character pattern of font type 6 and its Fourier transform plane.

		2		3		4		5				
0		6	6		7		8		9		1	
	\top	18	19	20	21	22	23	24	25		\neg	
10	11	26	27	28	29	30	31	32	33	14	15	
		34	35	36	37	38	39	40	41			
12	13	42	43	44	45	46	47	48	49	16	17	

Figure 8. The spatial frequency plane (upper half).

佬珪邸褂哦緊獄悠識釩椅肛骼経舍酸唇惜理祗 帷鏈鍋臅驟雙淮掬對仗撓螃勵幕役楊慧蓋繁卹 鳌條薩斫剜硬獸叩苔踩斃掄劉砸沬遛溝米釀啵 **출企產墜焉齦措鼙跑覆鯝粥鏗鉻詼喬曊嫡趁剜** 穢卅欖跚沾勇嵩矢殤雕成蓆謊皎仕鴣習氛念捎 稜昏依熟鍔腥迨訂擻把夭要芾彗地泅鷸誶鮪澎 儲哺附溥杷膊檜櫞膾逢型突籍譜闡瑁侑貴尋曼 故壅壺固言禍耀蹦蚜共終兹尢舛鍰蜂隋腸服隘 坤難跡柿慍鴿潡畔摰咩篾趙碩抉啼鴻墊阿循休 客崴牆瀞駭寧湮伉灰衢鴨泥蓬欺嫗攸餌劣桿關 答恍閱錦輻侯硏哎奢粽脈譏缺須厚婢藉方蹣阱 挑窩棵玟綰尾哇澈蠅召鹹沅玷觀中瓷衝鈣戍禦 咒翎椿倪灏慨甚氧飽聰霰澤惟孑擎潛捆孜酺哩 型譚崢嬤閭崇杠呻會卸隄矚奠笙糖梅嬈禦羿堠 就遏僵雲第粹您如警船避匍櫞鳴辦煥泠召鲍草 Figure 9. Some training characters.

在现代的资讯社會中每 天有大量的印刷品出版 諸如報纸期刊雜誌以及 辦公室的文件等文件中 有著不同的资料形態如

標題本文圖片等它們被 用來導引讀者去區分不 同的主題與內容爲了有 效率的存取文件中的資 訊便需要一套正確而有

效的文件自動輸入系統 這其中有關於文字的資 訊如大小顏色字形字體 等有別於經常被探討的 中文文字辨認而中文字 體辨認一直是沒被觸及 到的問題在有限的文獻 中英文字體辨認是採用 頻譜特徵及統計分析的 方法來解讀字體特性然

而傳統的統計式模式識別正面臨類神經網路的 挑戰其中尤以倒傳遞網 路的應用最普遍它的學 習精度高回想速度快理

體的特性得以正確的辨 認中文字體以下先說明 頻體特徵向量及倒傳遞 網路然後報告實驗結果 最後給一結論做為結束

Figure 10. The tested characters in the experiments.

	11111 11 1	1111111111	11111 11 1	3113111113	11111 11 1
1111111111	11111 11 1	11111111111	11111 11 1	11111111111	11111 11 1
4111531111	11311 11 1	4111511111	11111 11 1	1311531111	11311 11 1
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1113113111	11111 11 1	1113113111	11111 11 1	1113111113	13111 11 1
	21212 22 2	2222222662	22222 22 2	2222222252	22222 22 2
2225222552	25252 22 2	2222222652			
2522225255	2 2 2 2 5 2 2 2	222222222	22222 22 2	222222222	22222 22 2
2222252262	22226 22 2	2222222262	22226 22 2	222222262	22222 22 2
2522255226	22222 22 2	222222222	22222 22 2	222222222	22222 22 2
2222622222	22622 22 2	2262622222	22622 62 2	2222622222	22622 22 2
				2222622122	
3333634133	3 3 3 1 3 3 3	1333633133	33313 33 3	3333633133	33333 33 3
3633433634	3 3 3 3 3 3 3	3333433334	33333 33 3	3633336333	33333 33 3
1333363134	11334 33 3	1333333134	13334 33 3	3333333333	33333 33 3
3333331343	33333 33 3	3 3 3 3 3 3 1 3 4 3	33333 33 3	3333331333	33333 33 3
1333433333	13433 13 3	1333433333	13433 13 3	1333433363	33333 33 3
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444441441	44414 44 4	4444464441	44444 44 4	444444444	
4444414414	44444 44 4	443444414	43444 44 4	4436344444	43444 44 4
441444444	41444 44 4	4414444644	41444 44 4	444444344	44444 44 4
4444144144	44114 44 4	4444144114	44414 44 4	3443444414	44444 44 4
1444444444	44444 44 4	1444444434	44444 44 4	4444444444	44444 44 4
5555563535		5555563535	55555 55 5	5555565555	55555 55 5
5522255255	52255 55 5	555555555	55555 55 5	5522555255	52555 55 5
2555655552	55555 55 5	5555655555	55555 55 5	5555655552	55555 55 5
55555552556	55555 55 5	5555555656	55555 55 5		55555 55 5
5555255555	55555 55 5	5555255555	55555 55 5	5555255555	55555 55 5
6666636666	66366 66 6	6666636664	66366 66 6	6666636666	66666 66 6
6666636666	66366 66 6	6666636666	66366 66 6	6666636666	66666 66 6
6666656366	66666 66 6	6666662366	66666 66 6	6666662666	66666 66 6
6666662666	66666 66 6	6616662666	66666 66 6	6665662666	66626 66 6
6666666666	66666 66 6	6661666636	66666 66 6	6666656666	66666 66 6

Figure 11. The classification results obtained in the first experiment.

Figure 12. The classification results obtained in the second experiment.

Figure 13. The classification results obtained in the last experiment.