## OBJECT RECOGNITION USING TACTILE IMAGE ARRAY SENSORS

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## Abstract

The objective of this paper is to develop an object recognition system through the combination of 2-D tactile image array and visual sensors. A video camera is used to acquire a top view image of an object and two tactile sensing arrays mounted on a gripper are used to detect the tactile information about the lateral surfaces of the object. 3-D reference object models are established as a decision tree, and recognition of unknown objects is accomplished through measuring and comparing input object features hierarchically with these of the reference objects associated with the decision tree.

The clustering process and recognition procedures are described. The recognition scheme has been implemented. The resulting decision tree is also presented.

## I . INTRODUCPION

Conventionally, object recognition usually is performed using visual information. With the advent of tactile array sensors [1-3] also useful for object shape measurement, we propose in this paper a new approach to object recognition which combines the use of visual and tactile information. Non-visual information of object shapes is obtained from a video camera mounted right above the work platform, and tactile information of lateral object shapes is measured by two array sensors mounted onto the robot grippers. Both types of $2-\mathrm{D}$ shape information are utilized for recognition. The recognition scheme is defined in a hierarchical manner, so that an object is recognized first with the $2-D$ visual information along, followed by, if necessary, the 2-D tactile information measured when the object is grasped by the robot gripper.

The proposed approach will use moment invariants $[8,9]$ of object silhouette shapes as the features for object recognition. The reason for this is twofold. First, the lateral object shapes measured with the tactile array sensor are in low resolution because of the small array size available. Also, the shapes result from touching or taction of object surfaces on array sensor elements, so the number of points included in a shape ranges from one point (e.g., when the object is a sphere), a line (e.g., when the object is a cylinder), a surface patch (e.g., when the object is a polyhedron), to possibly a combination of the former three cases. The boundaries of such shapes, especially of the first two (a point and a line), are not meaningful enough for most
boundary-based shape descriptions (such as Fourier descriptors, chain codes, syntactic string representations, etc.) to be applicable here. Instead it is better to base the shape analysis on shape regions, and moment invariants are appropriate for this purpose. Next, since robot manipulation on the objects is necessary, it is of ten required to find out the position and the orientation of a given object so that proper grasp of the object with the robot gripper can be accomplished. For this, moments turn out to be the best choice. In particular, object centroids and principle axes, which defines object positions and orientations, can be easily derived as functions of low-order moments. The hierarchical recognition scheme is based on a decision tree [10] which can be constructed automatically in the learning phase from a set of given objects. Object shape ambiguity is resolved further as more tree levels are expanded until all shapes are discriminated or until furcher resolution is impossible. In the recognition phase, the decision tree is traversed when input objects features are compared with reference object features until a decisive tree node is reached or unitl the input object is determined indiscriminable in its current stable state. For the latter case, the gripper is operated to pick up and rotate the object so that a new object state can be obtained. Another phase of object recognition is then started again.

## II. SYSTEM CONFIGURATION AND TACTILE INFORMATION MEASUREMENT

A. System Configuration

The system we use for object recognition and manipulation is shown in Fig. l. Both the IV camera and the array sensors are controlled by a microcomputer. The camera is mounted right on top of a work platform on which objects are laid. It is assumed that the camera is far enough from the platform so the perspective effects on object images can be reduced to a minimum. The camera optical axis (going through the camera lens center) is made perpendicular to the platform plane.
The gripper we use includes two square-shaped $16 \times 16$ array sensors. The elements are attached close enough to the array edges so that slant contact of an object surface with any array edge can also be detected. The tactile information measured by touching an identical object from a fixed lateral direction (fixed with respect to the principal axis of inertia of the object, as will be discussed) will always be identical or stable.


Fig. 1. System Configuration for Object Recognition and Manipulation

Before the tactile information measurement process can be described, we define some notations to facilitate geometric descriptions of the system configuration. Let $A_{R}$ denote the right-hand side array sensor as viewed from the gripper wrist, and $A_{L}$ denote the left-hand side one. In some cases, $A_{R}$ and $A_{L}$ will also be used to specify the planes going through the sensing-element surfaces. Each array, after touching any object surface, will provide an array image of tactile information. Let $I_{R}$ denote the image provided by $A_{R}$ and $I_{L}$ provided by $A_{L}$. Let $O_{R}$ be the origin of the image coordinate system for $\mathrm{I}_{\mathrm{R}} \cdot \mathrm{O}_{\mathrm{R}}$ is chosen to be the center of $A_{R}$. The origin $O_{L}$ for $I_{L}$ is similarly chosen. The line going through $O_{R}$ and $O_{L}$ will be called the gripper lateral axis and denoted by $L_{L}$. Also, when $A_{R}$ and $A_{L}$ are opened apart to the maximum, the middle point of the line segment joing $O_{\mathrm{R}}$ and $\mathrm{O}_{\mathrm{L}}$ will be called the gripper center and denoted by $G$. The plane


Eig. 2 Spatial relation among various system planes, axes, and centers. " + " denotes positive directions of axes $L_{L}$ and $L_{C}$. The Object is being measured for its tactile information from direction $90^{\circ}$.
defined by the surface of the platform will be denoted by $P_{P}$. And the line going through $G$ and perpendicular to $P_{P}$ will be called the gripper vertical axis and denoted by $L_{V}$. The direction defined by the vector from $G$ to $O_{R}$ will be called the positive direction of $L_{L}$. Another useful structure is the plane going through $G$ and $L_{V}$, and perpendicular to $L_{L}$ (and so parallel to $A_{R}$ and $A_{L}$ ), which will be called the gripper central plane denoted by $P_{G}$. Fig. 2 shows the spatial relation among all the geometric structures defined above.
III. Overview on Object Learning and Recognition Schemes
A. Object Shape Learning

Accordingly, a $\frac{\text { block diagram showing the major }}{\text { din }}$ steps of the learning phase is included in Fig. 3 which needs some further explanation. After all the reference objects are discriminated according to their top-view silhouette boundaries, there may still exist some groups of objects, each containing several objects which are still visually indiscriminable. Then, for each such group, the gripper is operated to measure tactile information for further discrimination. This precedes by first selecting a set of preselected lateral directions and then measuring a pair of tactile images for each of these directions. The lateral direction most effective for discriminating each group of visually-ambiguous objects is selected. Stop if all groups of ambiguous objects are discriminable; repeat the process by selecting another most effective lateral direction from the remaining directions for each subgroup of still ambiguous objects until all lateral directions are tried. The above learning procedure also involves selection of shape features from visual and tactile object images for object discrimination. The result of learning will be a liferarchical decision tree with each tree node represented by a group of ambiguous or indiscriminable objects and each tree link associated with a most effective lateral direction $\theta$. The emphasis here is that the whole learning procedure can be made fully automatic.


Fig. 3 Flowchart of learning procedure


Fig. 4 Flowchart of recognition procedure

## B. Object Shape Recognition

As shown inf Fig. 4, the recognition procedure begins with taking the top-view visual image of a given unknown object after it is brought right under the TV camera on the platform. The object is then discriminated according to features extracted from the visual image. If the object is not discriminable with its visual image alone, a pair of tactile images are then measured from lateral direction specified in the decision tree. After object features are extracted, the object is discriminated further. This step may be repeated more than once if the number of tree levels is more than two. Most objects can be recognized after this step.

But as mentioned previously, there still exist objects which are indiscriminable if they are in certain stable states on the platform. One way to solve the problem is to change the stable state of the input object so that the originally "invisible" and "untouchable" object portion can become "visible" and "touchable."
IV. TACTILE AND VISUAL FEATURE SELECTION
A. Shape Features for Visual Recognition


#### Abstract

Since the TV camera can take images with a rather high resolution and since object silhouette boundaries reveal, in most cases, enough shape information for object recognition, the point set used for defining moments is chosen to include just the shape boundary instead of all silhouette points. This set will be denoted as BV. This also makes the features, to be defined next, more informative about minute details of the shape boundaries. Furthermore, moment computation can speed up significantly because much less points are involved. All features for


 recognizing visual images will be denoted as $v_{i}$.The first feature $v_{1}$ we use is $m_{00}=\overline{m_{00}}$ which is the area of $B V$. Since $B_{V}$ is the silhouette boundary, $v_{l}$ actually is the perimeter of the boundary [11]. another useful shape feature is shape elongateness or eccentricity. An eccentricity measure in terms of central moments is described in [12] as:

$$
\left.e=\left[\bar{m}_{02}-\bar{m}_{20}\right)^{2}+\overline{m m}_{11}^{2}\right] / \bar{m}_{00}
$$

The third feature $V_{3}$ we use is the normalized moment of inertia around the centroid defined as follows:


In the following sections, we use $V$ to denote the feature vector composed of the three features $V_{1}$ through $\mathrm{v}_{3}$ described above, i. e., $\mathrm{V}=\left[\mathrm{v}_{1}, \mathrm{v}_{2}\right.$, $v_{3}$ ]. $V$ will be called the visual feature vector.

## B. Shape Features for Tactile Recognition

Since tactile images $I_{L}$ and $I_{R}$ are measured with a much lower resolution, all non-zero points in $\mathrm{I}_{\mathrm{L}}$ and $I_{R}$ (resulting from contact of array sensing elements on the surfaces) will be used to compute the moment values. In the following, the non-zero points in $I_{L}$ and $I_{R}$ will be denoted as $B_{L}$ and $B_{R}$, respectively. Features extracted from $B_{L}$ and $B_{R}$ L $\quad \mathrm{R}$
will be denoted as $t_{i}$ and $t_{j}$ respectively, and called tactile features. Also, the moments $m_{p q}$
(or $\bar{m}_{p q}$ ) computed from $B_{R}$ and $B_{L}$ will be
 respectively.

Again, the areas of $B_{L}$ and $B_{R}$ can be used as tactile features.
So we select $\mathrm{t}_{1}^{\mathrm{L}}$ as $\mathrm{m}_{00}^{\mathrm{L}}=\bar{m}_{00}^{\mathrm{L}}$ and $\mathrm{t}_{1}^{\mathrm{R}}$ as ${ }_{m_{00}}^{R}=\bar{m}_{00}^{R}$. Next, since $B_{L}$ and $B_{R}$ are mesured with array sensors $A_{L}$ and $A_{R}$ fixed spatially in position with respect to the platform plane $P_{P}$. the locations of the centroids and the directions of the principle axes of $B_{L}$ and $B_{R}$ reveal a certain amount of $3-D$ structural information about the object. Therefore, we choose $L_{2}$ and $t_{3}$ to be $\bar{x}_{L}$ and $\bar{y}_{L}$
$t_{2}^{R}$ and $t_{3}^{R}$ to be $\bar{x}_{R}$ and $\bar{y}_{R}$, respectively, and $t_{4}^{L}$
and $t_{4}^{R}$ to be:


Finally, $t_{5}^{L}$ and $t_{5}^{R}$ are selected similarly to $v_{2}$
as follows:

$$
\begin{aligned}
L_{5}^{L} & =\left(m_{02}^{L}-m_{20}^{L}\right)^{2}+4\left(m_{11}^{L}\right)^{2} / m_{00} \\
t_{5}^{R} & \left.=\left(m_{02}^{R}-m_{20}^{R}\right)^{2}+m_{11}^{R}\right)^{2} / m_{00}
\end{aligned}
$$

The two vectors $T^{L}=\left[\begin{array}{ccc}L \\ L_{1}\end{array}, L_{2}^{L}, t_{3}^{L}, t_{4}^{L}, t_{5}^{L}\right]$, and $T^{R}=\left[\begin{array}{ccccc}R & t_{1}, & t_{2}, & t_{3}^{R}, & t_{4}^{R}, \\ t_{5}^{R}\end{array}\right]$, together will be
called the tactile feature vector and will
be collected vector $T=\left[T^{L}, T^{R}\right]^{\prime}$.

## V. REFERENCE OBJECT LEARNING

## A. Decision Tree Construction Overview

Let the set of reference objects be denoted by $R_{1}, R_{2}, \ldots, R_{m}$. For each object $R_{1}$, there may exist more than one stable state. Each stable state actually should be, from the view point of object recognition, regarded as distinct $3-$ D object shape. In the following the $3-D$ shape of the $j$ th state of the ith object $R_{1}$ will be denoted as $S_{i j}$. Once an unknown input shape is recognized to be a parcicular $S_{i j}$, we can conclude that it is just the jth stable state of object $R_{i}$. Let $S$ denote the set of all the $3-D$ shapes, i.e., $S=\left\{S_{i j} \mid i=1,2\right.$, $\left.\ldots, m, j=1,2, \ldots, n_{i}\right\}$. Then the decision tree construction may be regarded as a consecutive partitioning of $S$ into sinaller subsets, with each level of parcitioning based on either the visual or the tactile shape features, until $S$ is partitioned into all non-partitionable subsets. Each subset of $S$ is partitioned into smaller subsets according to a clustering procedure. Thus, the decision tree has $S$ as its root and all non-partitionable sets as its leaf nodes.

A non-partitionable set as a leaf node is either a single-element set or a multiple-element set. The former case means that the single element, say $S_{i j}$, in the set can be uniquely discriminated from other $3-D$ shapes in $S$. And the later case means that any two $3-D$ shapes in the multiple-element set are indiscrimfnable from each other using the visual feature vector and the tactile feature vector pair measured from any lateral direction. On the other hand, all non-leaf tree nodes are multiple-element subsets of $S$. In the following, we use $S_{1}, S_{2}, \ldots, S_{n}$ to denote the $n_{1}$ first-level child nodes
of the decision tree, $S_{1.1}, S_{1.2}, \ldots, S_{1 . n_{1.2}}$ to denote the $\mathfrak{n}_{1,2}$ second-level child nodes $S_{1}$, and so on. In general, $S_{i_{1}}, 1_{2}, \ldots, i_{m-1}, i_{m}$
denote one of the $n_{1} .2 \ldots m$ mth-level child nodes of $S_{i_{1}}, i_{2}, \ldots i_{m-1}$.
B. First-Level Partitioning Based on Visual

Featire Vector
The first-level partitioning is always based on the visual feature vector. The reason for this is to obtain the most effective first-level partitioning because the visual shape is measured with a much higher resolution than the tactile shape. Note that the faster the set $S$ is decomposed into single-element subsets (i.e., the fewer the tree levels are), the faster the recognition based on the resulting decision tree will be. Let $S_{i}\left(i=1,2, \ldots, n_{1}\right)$ be a resulting first-level node. Then, $S_{1}$ includes all those 3-D shapes in $S$ which have a specific similar visual feature vector. this common feature vector for all shapes in $S$ which have a specific similar visual associated with the tree link from $S$ (the tree root) to $S_{i}$. $V_{i}$ will be used in the recognition phase for visual feature matching.
C. Multiple-Level Partitioning Based on Tactile Feature Vectors

The remaining levels of partitioning are based on the tactile feature vector pairs measured from a predetermined set $H$ of lateral directions. $H$ is determined in this study to include angles $\theta$ which are multiples of $30^{\circ}$, with $\theta_{0}=0^{\circ}$
coincident with the direction of the direction of the principal axis of the top-view shape. Therefore, $H=\left\{\left.\theta\right|_{\theta}=\mathbf{i} \times 30^{\circ}, \mathbf{i}=0,1, \ldots\right.$, 5\}. Note that only $\theta_{i}$ up to $180^{\circ}$ needs to be included because each time two lateral sides are measured. Practical choice of $H$ depend on the surface properties of the objects to be recognized. In general, we assume that $H$ include d lateral directions. In the following, we describe how to partition each first-level node $S_{i}\left(i=1,2, \ldots, n_{1}\right.$ ) into multiple levels of child nodes. Each level of partitioning will be made most effective according to a certain effectiveness measure defined subsequently. First, from each lateral direction $\theta_{\ell}$ in $H, \ell=1$ , ...., $d$, we measure the tactile feature vector pair for each 3-D shape in $S_{i}$.

Based on the resulting feature vector pairs, $S_{i}$ can be partitioned into a set of second-level child nodes denoted as $S_{i .1}^{\ell}, S_{i .2}^{\ell}, \ldots$, $S_{1 . n_{1.2}}^{l} S_{1 . j}^{\ell}$ are different lateral directions $\theta_{\ell}$ in $H$ set $P_{i}$, defined as

$$
\begin{aligned}
P_{i}^{\ell} & =\left\{s_{i . j}^{\ell} \mid j=1,2, \ldots, \stackrel{n}{n}_{\ell}^{\ell}\right\} \\
\mathbf{i} & =1,2, \ldots, n_{1}, \ell=1,2, \ldots, d,
\end{aligned}
$$

be used to denote such a partitioning. $A 11 P_{i}^{\ell}$
will be called the basic partitioning of $S_{i}$ Each $\mathrm{P}_{1}^{\ell}$ is a candidate for the final secondlevel partitioning. Let $\# P_{i}^{\ell}$ denote the number of nodes $S_{i . j}^{\ell}$ in $P_{i}^{\ell}$.
Obviously, the larger the number $\# \mathrm{P}_{i}^{l}$ is, the more effective the measured tactile features from direction $\theta_{\ell}$ are for shape discrimination (because the shapes in $S_{1}$ are separated into more groups). Therefore, we define $\# P_{i}^{\ell}$ as the effectiveness measure lateral direction $\theta_{\ell}$.
Then, we can now choose the basic partitioning
$P_{i}^{\ell} i_{i t h}$ the most effective lateral
direction $\theta_{\ell_{i}}$ as the desired second-level
partitioning of $S_{i}$ for use in the final decision
tree. We add a subscript i to the index $\ell_{i}$
of the most effective direction $\theta_{\ell_{i}}$ for $S_{i}$ to
emphasize the dependency of $\ell_{i}$ on $\stackrel{i}{S}_{i}$. Therefore, for each first-level node $S_{l}{ }_{l}$ in the decision
tree, we now have ${S_{i}}_{\ell_{i}}, S_{i}^{\ell_{i}}, \ldots, S_{i}^{\ell}, \ldots, n_{1.2}$
as its child nodes which are in the second level of the tree. Also, the lateral direction $\theta_{\ell_{i}}$, and the corresponding tactile feature vector pair, denoted as $T_{i} . j$, will be said to be associated with the tree link from $S_{i}$ to $S_{i . j}^{\ell_{i}}, j=1,2, \ldots,{ }_{1}{ }_{1.2}$. They will be used in the recognition phase for tactile information measurement and feature matching. This completes the second-level tree node generation.

To partition any second-level multiple-element node $S_{i j}$ further, we have to select the most effective lateral direction $\theta_{\ell_{1 . j}}$ from all those
in $H$ except the one $\theta_{\ell}$ already used in partitioning $S_{i}$. To obtain the partitioning $P_{i . j}^{\ell}$ defined similarly to $\mathrm{P}_{\mathrm{i}}^{\ell}$ as

$$
P_{i . j}^{\ell}=\left\{s_{i . j . k}^{\ell} \mid k=1,2, \ldots, n_{1.2 .3}^{\ell}\right\}
$$

for $S_{1 . j}$ for a fixed $\theta_{\ell}$, the basic partitioning $P_{i}$ can be utilized to speed up the process. Actually two shapes in $S_{1 . j}$ should be separated into two
distinct $S_{i . j . k}^{\ell}$ if the two shapes appear in two different $S_{i . j}^{\ell}$ in $P_{i}^{\ell}$ (i.e., the two shapes are
dissimilar according to their tactile feature vector pairs measured form lateral direction $\theta_{\ell}$ ).
Once $P_{1 . j}^{\ell}$ for all $\theta_{\ell}$ (except $\theta_{\ell_{i}}$ ) are obtained,
the remaining steps to generate the third-level tree nodes are all the same as those for generating the second-level ones.

Finally the above process for generating the third-level nodes is repeated to generate all the nodes of lower levels, if necessary, until every tree node is found to include just a single shape (or several shapes but all from a single object), or until no more lateral direction from $H$ is available for partitioning any multiple-element tree node. This completes the construction of the decision tree.

## VI. EXPERIMENTAL RESULTS

A $16 \times 16$ simulated tactile image is used to conduct the experiment at this stage. Visual images are acquired with a TV camera. Fig. 5 shows the sketches of the ten objects chosen as the test sets. they include most angular and curved surfaces encountered in common industrial applications.

Each stable state of an object was considered to be a separate entity by itself. Therefore, the recognition problem consisted of being given an unknown object, taking its visual image and tactile images as required, and then determining what object it is and in which stable state it lies. A cross reference table (Table 1) is included which transposes between the actual object names and stable states and the object names indicated in the decision tree. The top views (visual shapes) of the stable states of some objects do not possess principal axis owing to their rotational symmetry. Such object states are not included in the experiment. Treatment of rotationally symmetric shapes has been studied in another research [13]. The resulting decision tree is shown in Fig. 6.

## VII CONCLUSIONS

We have demonstrated the feasibility of a system that utilizes a combination of visual information and taction in the identifcation and discrimination of three dimensional objects.

A recognition scheme has been implemented which succeeds in identifying any of the ten reference objects placed in any of their permissable stable states. Although the decision tree was constructed using these objects in four specified orientations as the "Training Set", the "Test Set" consisted of objects placed in random orientations
and this scheme successfully identified all these stable states with satisfactory accuracy.

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tal object 1

(d) object 4

(b) object?

(a) corececs

(c) object 3
(t) ousece :
(g) cblect

(m) oosect:

(1) obstet 9

Fig. 5 Sketches of reference objects used in experiments

| bbuect mant in tree | Corresponoing poject mimber | stable state |
| :---: | :---: | :---: |
| $\wedge$ | 7 | a |
| ) | 8 | a |
| 6 | 8 | c |
|  | 9 | a |
| F | 9 | \% |
| a | 9 | c |
| ${ }^{H}$ | 2 | a |
| $J$ | 6 | a |
| K | ${ }_{6}^{6}$ | c |
| $\stackrel{H}{1}$ | 10 | a |
| N | 10 | b |
| 0 | 10 | c |
| P | 10 | d |
| 0 | 3 | a |
| R | 4 | ${ }^{\text {a }}$ |
| \$ | 1 | b |
| $\stackrel{1}{1}$ | 1 | ${ }_{c}$ |
| $\stackrel{y}{V}$ | 1 | d |
| N | 1 | * |
| $x$ | 5 | a |
| $\underline{y}$ | 5 | b |
| ${ }_{c}^{1}$ | 5 9 | ${ }_{\text {c }}$ |
| DD | 7 | c |
| EE |  | d |
| FF | 7 | e |

Table 1 Cross reference table for object names and stable states.


Fig. 6 Decision tree constructed in the experiment

