



National Yang Ming Chiao Tung University
Computer Architecture & System Lab

Paging

IOC5226 Operating System Capstone

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Acknowledgements and Disclaimer

- Slides were developed in the reference with
 - MIT 6.828 Operating system engineering class, 2018
 - MIT 6.004 Operating system, 2018
 - Remzi H. Arpaci-Dusseau etl. , Operating systems: Three easy pieces. WISC



Outline

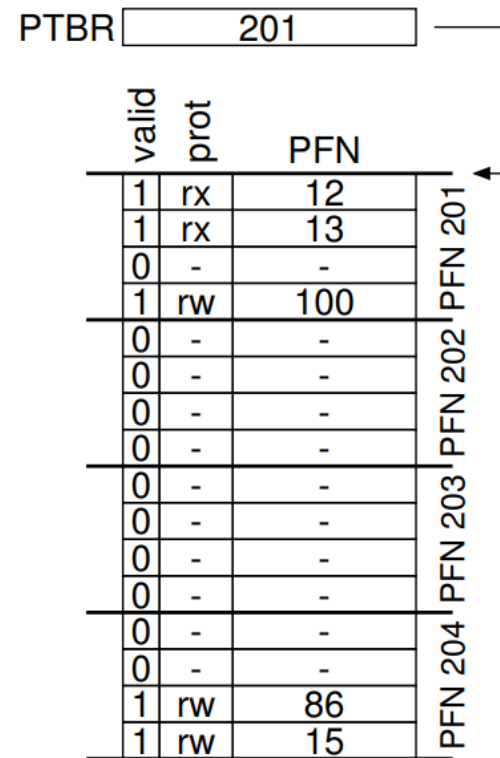
- Paging
 - Multi-level page table
 - Demand paging
 - The inverted page table
 - Page sharing



Page table (linear structure)

- Page table (linear structure) can be vary large !
 - 32-bit address (2^{32} bytes), 4KB (2^{12} bytes) pages, 4B PT entry
 - The number of page is ($2^{32}/2^{12} = 2^{20}$),
 - One page table size is $2^{20} \times 4$ bytes = 4MB per process
 - Hundreds of processes -> Hundreds of MB for PT

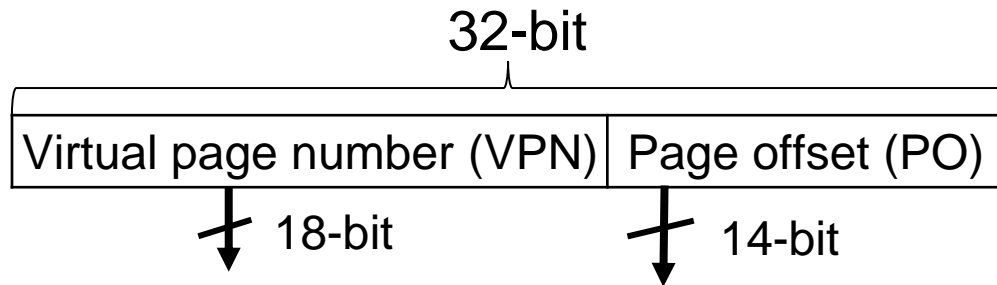
Linear Page Table





Bigger pages

- A 32-bit address, but increase page size from 4KB to 16KB
 - Each PTE is 4 bytes and now we have 2^{18} entries in our page table
 - The total size of a page table is ($2^{18} \times 4$ bytes = 1MB)
 - The page table size (4MB in case 4 KB page size)
- What problems are shown with this approach ?
 - **Internal fragmentation** (big pages lead to waste within each page)





Page size

- **Arguments for larger page size**
 - Leads to a smaller page table
 - May be more efficient for disk access (block size of disk)
 - Larger page size – TLB entries capture more addresses per entry (why?), so there are fewer misses, with the “right” locality
 - X86 page sizes: 4KB, 2MB, 4MB ...
- **Arguments for smaller page size**
 - Conserve storage space – less fragmentation (why?)



Multi-level page tables

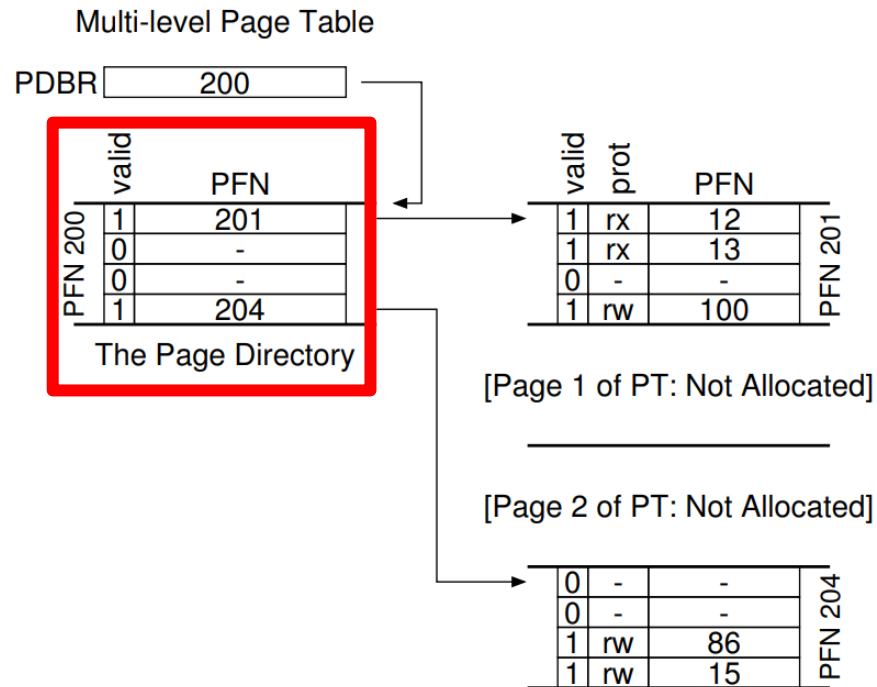
- Turn page table into a tree (hierarchy) structure
 - Aim to reduce the memory space requirement to store page table
 - Divide page table (PT) into page sized chunks
 - Hold only the part of PT where PT entries are valid
 - Directory points to portions of the PT
 - Directory says where to find PT or that chunk is invalid



Multi-level page table (cont.)

- **Multi-level page table**

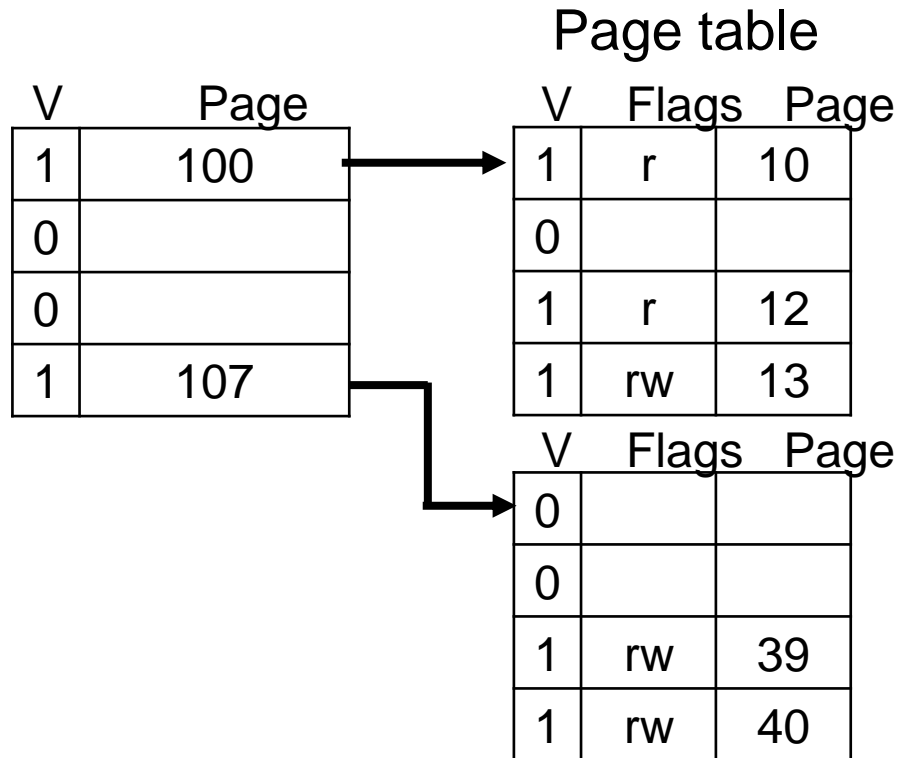
- Chop up the page table into page-sized units
- **Page directory** tells where a page of the page table is
 - A number of **page directory entries (PDE)**
 - A **page frame number (PFN)**, and a valid bit





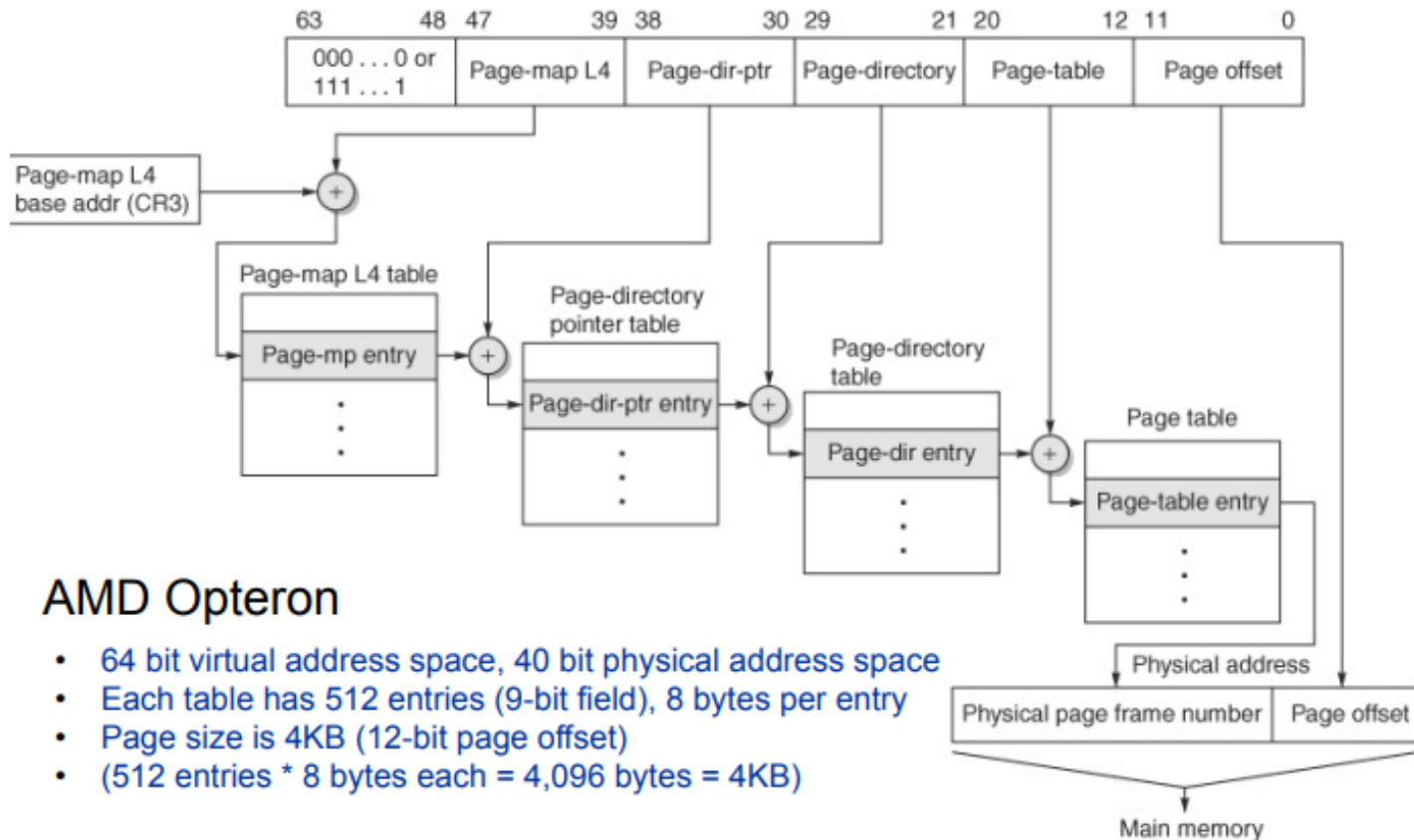
Multi-level page table (cont.)

- What are the advantages of multi-level page table?
 - Only allocate “using” page-table space
 - Compact and supports **sparse** address space





Multi-level paging table (cont.)





Important formula for paging table

- Number of entries in page table
 - $(\text{virtual address space size}) / (\text{page size}) = \text{number of pages}$
- Virtual address space size
 - 2^n Bytes
- Size of page table
 - $(\text{Number of entries in page table}) \times (\text{size of PTE})$



Case study of multi-level paging table

- How many levels of page tables would be required ?
 - A virtual memory system with physical memory of 8 GB, a page size of 8 KB, 46 bit virtual address, and PTE size is 4 B
- Initially
 - Page size = 8 KB = 2^{13} B
 - Virtual address space size = 2^{46} B
 - PTE = 4 B = 2^2 B
 - Number of pages or number of entries in page table
= 2^{46} B / 2^{13} B = 2^{33}
 - Size of page table = $2^{33} \times 2^2$ B = 2^{35} B



Case study of multi-level paging table (cont.)

- How many levels of page tables would be required ?
 - A virtual memory system with physical memory of 8 GB, a page size of 8 KB, 46 bit virtual address, and PTE size is 4 B
- Now, size of page table $>$ page size (2^{35} B $>$ 2^{13} B)
 - Create one more level
 - Number of page tables in last level
$$2^{35} \text{ B} / 2^{13} \text{ B} = 2^{22}$$
 - Size of page table [second last level]
 - $2^{22} \times 2^2 \text{ B} = 2^{24} \text{ B}$



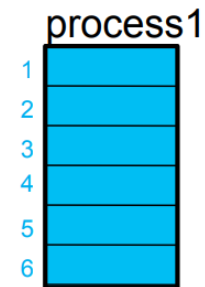
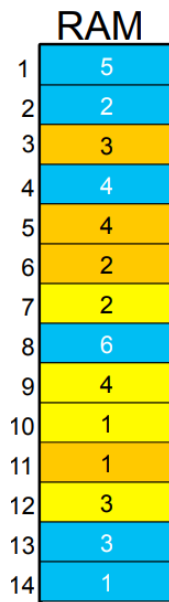
Case study of multi-level paging table (cont.)

- How many levels of page tables would be required ?
 - A virtual memory system with physical memory of 8 GB, a page size of 8 KB, 46 bit virtual address, and PTE size is 4 B
- Now, size of page table $>$ page size (2^{24} B $>$ 2^{13} B)
 - Create one more level [third last level]
 - Number of page tables in second last level
 $= 2^{24}$ B / 2^{13} B = 2^{11}
 - Size of page table [third last level]=
 $= 2^{11} \times 2^2$ B = 2^{13} B = page size



Virtual memory

- Do we need to load all blocks of the page table into main memory before the process starts executing ?
 - **No !!**
 - Some code may not even be executed
- How to reduce the loading of unnecessary pages ?



process page table

| block | page frame |
|-------|------------|
| 1 | 14 |
| 2 | 2 |
| 3 | 13 |
| 4 | 4 |
| 5 | 1 |
| 6 | 8 |



Demand paging

- **Demand paging**
 - Pages are loaded from disk to RAM, **only when needed**
- **Why demand paging ?**
 - Reducing I/O
 - More users and decrease the number of memory requests
- **Pure demand paging**
 - When no pages are loaded into memory initially, pages generates page faults. No prediction !!
- **Pre-paging**
 - Predict which pages will be used and swap them into the RAM



Demand paging

- **How does demand paging work ?**
 - Using **present bit** in process page table to indicate if the block is in RAM or not
 - The process issues a page fault interrupt if an accessed page is not present in RAM
 - The OS loads the page into RAM and mark the present bit to 1
 - The OS removes another block from RAM if no pages on RAM are free



Demand paging implementation

- Keep copy of process's pages on disk, some are in RAM
 - Extend page table to include “**present**” and “**valid**”
 - Access to “page out” data by using **trap**
- **Inside the trap handler**
 - Access pages that are temporarily paged out to disk
 - Allocate a physical page frame to hold contents (might require another page to be paged out)
 - Copy data from disk to allocated page frame (**slow!!**)
 - Update page table entry
 - OS schedules processes



Effective access times (EAT)

- **EAT is used to measure the performance of demand paging**
- **Parameter**
 - p: page fault rate; ma: memory access time; pft: page fault time
 - $EAT: (1 - p) \times ma + p \times pft$
- **Discussion**
 - The EAT is proportional to page fault time



Effective access times (EAT)

- **What is average access latency ?**
 - L1 cache: 2 cycles
 - L2 cache: 10 cycles
 - Main memory: 150 cycles
 - Disk: 10 ms -> 30, 000, 000 cycles on 3.0 GHz processor
- **Assume access having following characteristics:**
 - 98% handled by L1 cache
 - 1% handled by L2 cache
 - 0.99% handled by DRAM
 - 0.01% cause page fault
 - What's the average access latency ?



Effective access times (EAT)

- **Assume access having following characteristics:**
 - 98% handled by L1 cache
 - 1% handled by L2 cache
 - 0.99% handled by DRAM
 - 0.01% cause page fault
 - What's the average access latency ?
- **Average access latency:**
 - $(0.98 \times 2) + (0.01 \times 10) + (0.99 \times 150) + (0.0001 \times 30,000,000) = 1.96 + 0.1 + 1.485 + 3000 = \text{about } 3000 \text{ cycles / access}$
- Need **LOW** page fault rates to sustain performance !!



More issues

- **Page selection policy**
 - When do we load a page ?
- **Page replacement policy**
 - What pages do we swap to disk to make room for new pages ?
 - When do we swap pages out to disk ?



Page selection policy

- **Demand paging**

- Load page in response to access (page fault)

- **Pre-paging (prefetching)**

- Predict what pages will be accesses in near future
- Prefetch pages in advance of access
- Problems
 - Hard to predict accurately
 - Mispredictions can cause useful pages to be replaced



Page replacement policies

- **Random**
- **FIFO** (first in, first out)
 - Throw out oldest pages
- **Optimal**
 - Throw out page used farthest in the future
- **LRU** (least recently used)
 - Throw out page not used in the longest time
- **NFU** (not frequently used)
 - Do not throw out recently used pages



Demand paging issues

- **Performance**

- Need lots of locality -> otherwise run at disk speeds
 - If most accesses are to data already in DRAM -> great !
 - **Spatial locality**: often access “nearby” addresses
 - **Temporal locality**: Often re-access same addresses again and again
- How to resume a process ?
 - Re-execute instruction? Only if no side effects !
- Run other processes / threads while serving the page fault



Belay's Anomaly

- Belay's anomaly
 - For some replacement algorithms
 - **MORE** pages in main memory can lead to **MORE** page faults !!
- **Example:**
 - FIFO replacement policy
 - Reference string: A B C D A B E A B C D E
 - Three pages -> 9 faults
 - Four pages -> 10 faults
 - Adding more memory might not help for page faults in some replacement algorithms



Thrashing

- **Working set**
 - Collection of memory currently being used by a process
- **Thrashing**
 - If all working sets do not fit in memory
 - One “hot” page replaces another
 - Percentage of accesses that generate page faults skyrockets
- **Typical solutions**
 - “swap out” entire processes
 - Invoked when page fault rate exceeds some bound
 - Linux invokes the out-of-memory (OOM) killer



Inverted page tables

- **Multi-level page table**

- The number of levels is increased as the size of virtual memory address space grows
- Given 64-bits address space, 4-KB page size, a PTE of 4 bytes, each page table can store 1024 entries
- 6 ($\text{ceil}(52/10)$) levels are required
- 6 memory accesses for each address translation

- **Observation of the inverted page table**

- Size of physical memory is much smaller
- The inverted page table only has entries corresponding to actual physical frames



Inverted page tables

- **Inverted page table**

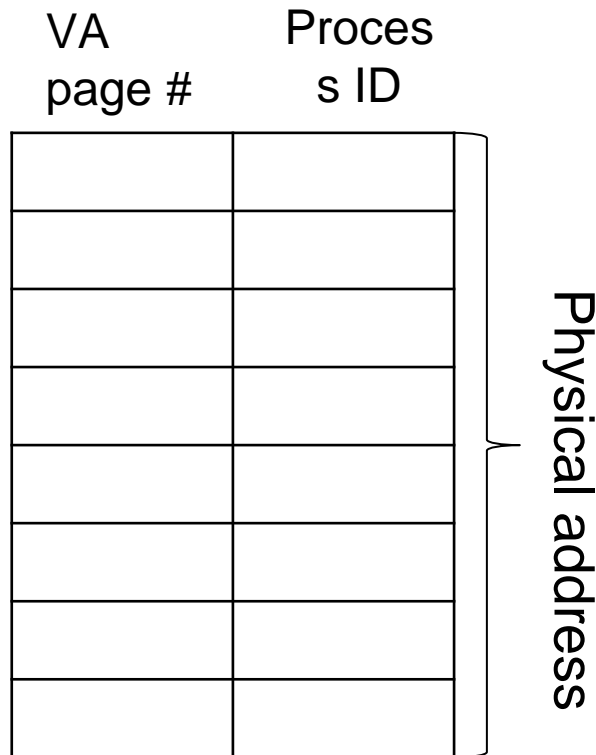
- Aim to create a page table for all processes
- The inverted page table stores physical frame
- Each page table entry record which used pages for user processes
- The page table include process ID and page number
- Search problem in an inverted page table



Inverted page table

- **Simple Inverted page table**

- **The number of page table entries (PTE) = the number of physical frames**
- Each PTE contain the pair <process ID, virtual page #>
- Translate a virtual address, compare each <process ID, virtual page #> against each entry
- If a match is found, the inverted page table index is used to obtain physical address

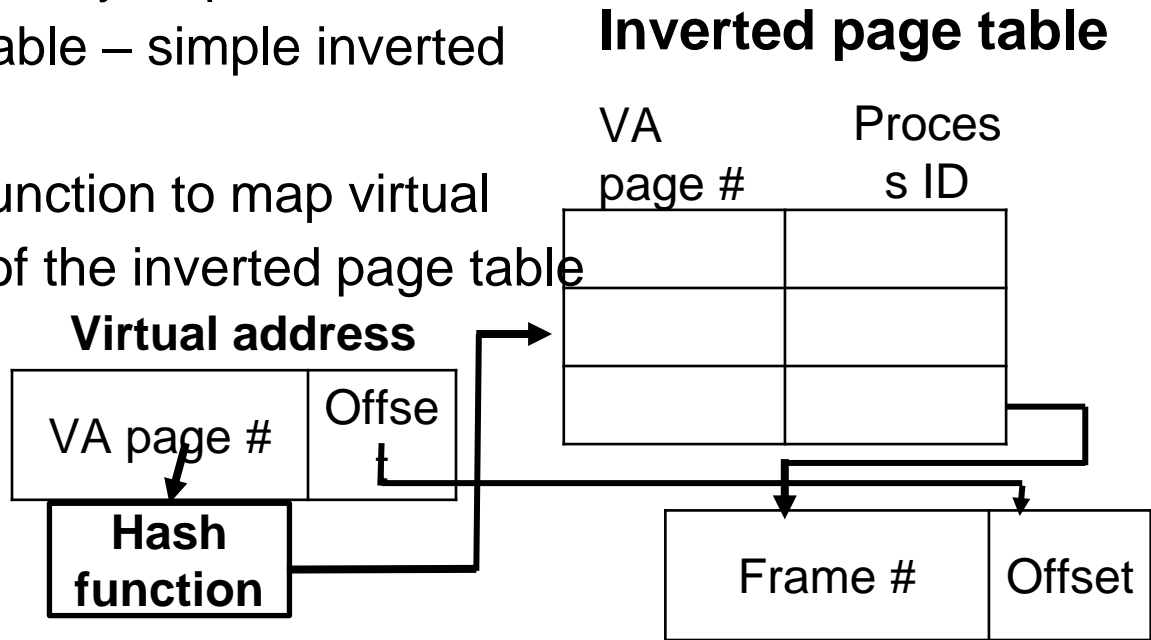




Inverted page table

- **Hashed inverted page table**

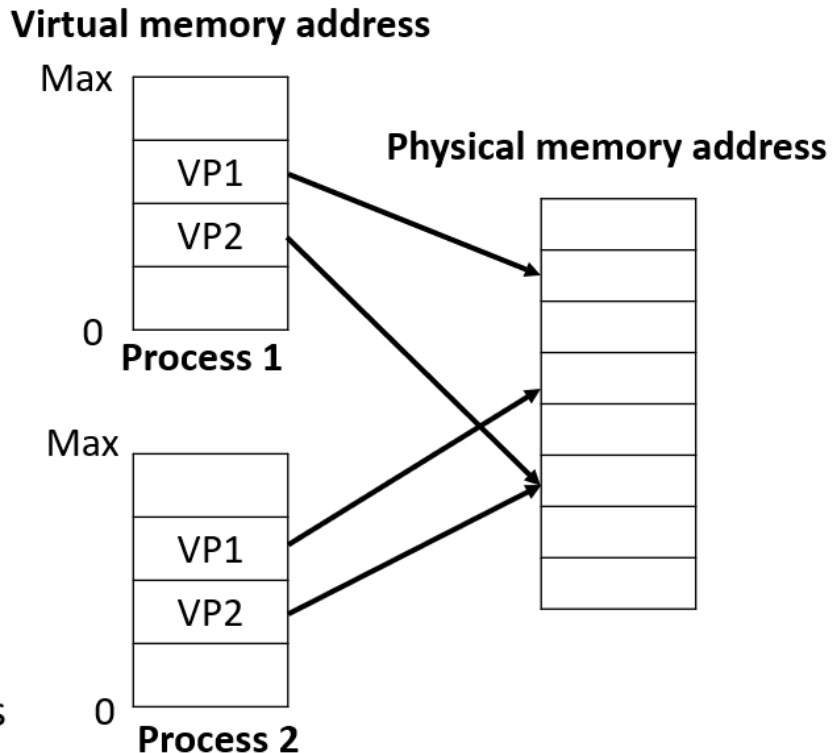
- Finding a match may require to scan through entire table – simple inverted page table
- Using hashed function to map virtual page # to PTE of the inverted page table





Sharing pages

- How to share memory?
 - Entries in different process page tables map to the same PPN
 - Each process can have its own registers and data
 - There can be only one copy of data kept in physical memory, such as shared library
 - Each process's page table maps ; onto the same PPN





Conclusion

- Multi-level page table
 - Reduce the page table
- Demand paging
 - Reduce I/O, load data from disk to memory when it is needed
- Effective access time (EAT)
 - Measure the performance of demand paging
- Page replacement
- Inverted page table
- Page sharing



Takeaway Questions

- What are purposes of the multi-level paging?
 - (A) Increase the number of pages can be used
 - (B) Reduce the memory space requirement to store page table
 - (C) Decrease the latency of the page table access
- How to reduce the number of unnecessary page access?
 - (A) Multi-level page table
 - (B) Page sharing
 - (C) Demand paging



Takeaway Questions

- How to reduce effective access time (EAT) ?
 - (A) Reduce the number of page faults
 - (B) Reduce page size
 - (C) Using the multi-level page table
- What are problems of an inverted page table?
 - (A) Increase the virtual page size
 - (B) The physical frame size is large
 - (C) Costly PTE search