

## Bonus2 - Sounds like a Network Problem, right?

Time Limit: 20 secs.

### Problem Description

Consider a simple undirected graph consisting of  $n$  vertices and  $m$  edges. Each vertex  $i$  is associated with a non-negative integer value  $w_i$ , and the weight of each edge  $(u, v) \in E$  is defined as

$$W_{u,v} := \|w_u \otimes w_v\|,$$

where  $\otimes$  is the bitwise exclusive-or (XOR) operation and  $\|x\|$  is the number of 1s in the binary representation of  $x$ .

In addition, we're given  $q$  constraints on the value  $w_i$  for  $1 \leq i \leq n$ , where each constraint is represented as a 5-tuple  $(t, u, i, v, j)$ , where  $t \in \{0, 1\}$  and

- if  $t = 0$ , then  $\text{bit}(w_u, i)$  must equal  $\text{bit}(w_v, j)$ ,
- if  $t = 1$ , then  $\text{bit}(w_u, i)$  must not equal  $\text{bit}(w_v, j)$ ,

and  $\text{bit}(x, i)$  denotes the  $(i + 1)^{\text{th}}$  least significant bit in the binary representation of  $x$ . For example,  $\text{bit}(12, 1) = 0$  and  $\text{bit}(12, 2) = 1$ .

However, some values associated with some vertices are lost. Your task is to assign new values to these vertices such that  $\sum_{(u,v) \in E} W_{u,v}$  is minimized while the  $q$  constraints are also satisfied.

### Input Format

The first line consists of two integers  $n$  and  $m$ , the number of vertices and the number of edges. Each of the following  $m$  lines consists of two integers  $u, v$ , indicating that there is an edge between  $u$  and  $v$ . The next line contains  $n$  integers, indicating the values associated with each vertex. The value of  $-1$  indicates that the value was lost.

The next line contains an integer  $q$ , the number of constraints. Each of the following  $q$  lines contains five integers  $t, u, i, v, j$ , the parameters associated with each constraint.

You may assume that

- The vertices are numbered from 0 to  $n - 1$ .
- $1 \leq n \leq 1000$ .
- $1 \leq m \leq 5000$ .
- $0 \leq w_k < 2^{16}$  for all  $1 \leq k \leq n$ .
- $0 \leq q \leq 8$ .
- $0 \leq i, j < 16$ .

## Output Format

Print the minimum possible value of  $\sum_{(u,v) \in E} W_{u,v}$  in a line. If it is not possible to satisfy all the constraints, print  $-1$  instead.

### Sample Input 1

```
4 4
1 3
1 2
3 2
0 3
-1 -1 60091 51514
2
1 2 0 1 5
0 2 6 0 15
```

### Sample Output 1

```
13
```

### Sample Input 2

```
3 2
0 1
1 2
-1 -1 -1
2
1 2 0 1 5
0 1 5 2 0
```

### Sample Output 2

```
-1
```

## Note.

Use bit-operators like  $\&$ ,  $\wedge$ , and  $\gg$  in C/C++ for the bit operations needed in this problem.

## Hint.

Notice that  $q$  is very small, and we can afford exhaustively trying all possibilities w.r.t. the  $q$  constraints. Understand what the definitions mean. Consider each bit separately and derive a suitable problem formulation.