

# Multimedia Communications

## @CS.NCTU

Lecture 14: Wireless Basics

Instructor: Kate Ching-Ju Lin (林靖茹)

# Outline

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- **SNR and capacity**
- Channel fading and path loss
- Modulation and coding scheme
- Rate adaptation
- Wireless multicasting

# SNR

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- Wireless channel

$$y = x + n$$

received signal    transmitted signal  
noise

- Signal-to-noise ratio (SNR)

$$\frac{\text{Power of the signal}}{\text{Power of the noise}} = \frac{\mathbb{E}[x^2]}{\mathbb{E}[n^2]} = \frac{P}{N_0}$$

- Unit of the power: watt

# SNR in decibels

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$$P_{\text{dBm}} = 10 \log_{10} P$$

$$N_{\text{dBm}} = 10 \log_{10} N_0$$

$$\begin{aligned} \Rightarrow \text{SNR}_{\text{dB}} &= 10 \log_{10} \frac{P}{N_0} \\ &= 10 \log_{10} P - 10 \log_{10} N_0 \\ &= P_{\text{dBm}} - N_{\text{dBm}} \end{aligned}$$

- dBm: unit of **power**
- dB: unit of **power difference**
- Example: noise = -90dBm, signal = -70 dBm
  - $\text{SNR}_{\text{dB}} = -70\text{dBm} - (-90\text{dBm}) = 20\text{dB}$
- Why using decibel?
  - Many signals have a wide dynamic ranges

# SINR

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- Signal-to-noise-plus-interference ratio

$$\text{SINR} = \frac{P}{I + N_0}$$

$$\text{SINR}_{\text{dB}} = 10 \log_{10} \frac{P}{I + N_0}$$

- Example: if there exist two interferers

$$y = x + i_1 + i_2 + n$$

$$\Rightarrow \text{SINR} = \frac{\mathbb{E}[x^2]}{\mathbb{E}[(i_1 + i_2 + n)^2]}$$

$$= \frac{\mathbb{E}[x^2]}{\mathbb{E}[i_1^2] + \mathbb{E}[i_2^2] + \mathbb{E}[n^2]}$$

If  $i_1, i_2, n$  are i.i.d

# Channel Capacity

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- Derived by Claude E. Shannon during World War II
- Assume that we have an additive white Gaussian noise (AWGN) channel with bandwidth  $B$  Hz

$$\text{Capacity (bit/s)} = B \log_2(1 + SNR)$$

- Also known as Shannon capacity
- SNR is expressed as a power ratio, not in decibel (dB)

# Outline

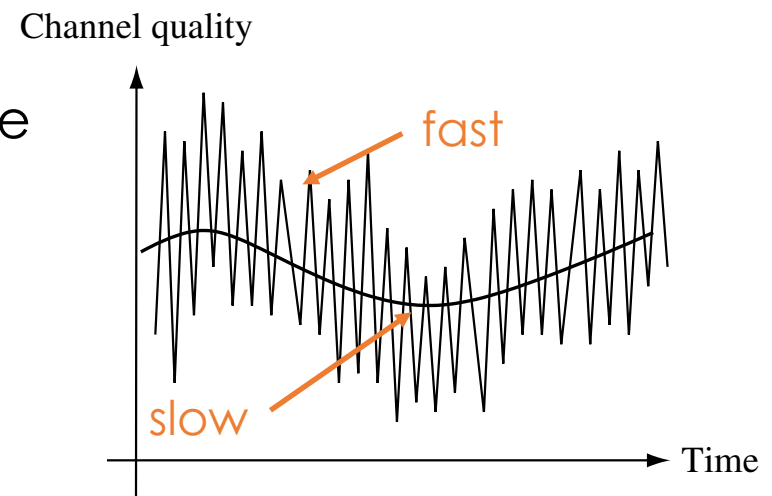
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- SNR and capacity
- **Channel fading and path loss**
- Modulation and coding scheme
- Rate adaptation
- Wireless multicasting

# Channel fading

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- Coherence time
  - The time over which a propagating wave may be considered **coherent**
- Fading
  - **Variation** of attenuation of a signal due to environmental dynamics, such as time, location, radio frequency and/or multi-path propagation
- Slow and fast fading
  - fast fading: if the coherence time is much shorter than the delay requirement of the application
  - slow fading: if the coherence time is longer.

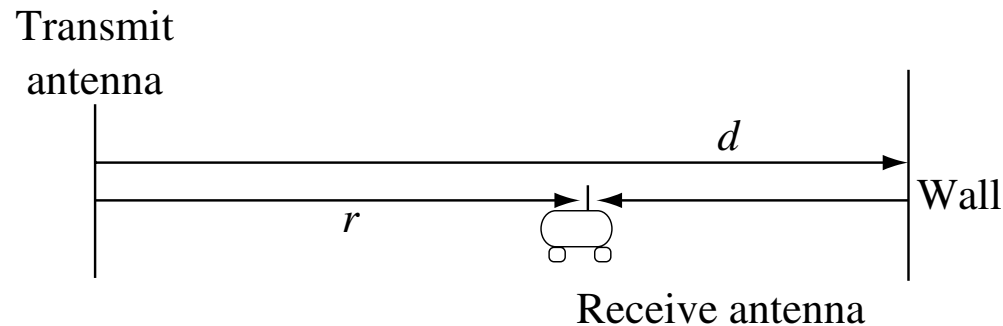




# Channel Fading

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- Fast fading usually caused by
  - High mobility (Doppler spread)
  - Multipath effects



- Slow fading usually caused by
  - Small/slow mobility
  - Shadowing (signal power fluctuates due to obstacles)

# Path Loss

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- Signal attenuation as the wave propagates over the air

$$PL = \frac{P_{rx}}{P_{tx}}$$

$$\Rightarrow P_{rx, \text{ dBm}} = P_{tx, \text{ dBm}} + PL_{\text{dB}}$$

- Example: assume the transmit power is 15dBm and the path loss is -90 dB
  - What is the receive power?  
→  $15\text{dBm} + (-90\text{dB}) = -75\text{dBm}$
  - What is the SNR if noise level is -90dBm?  
→  $-75\text{dBm} - (-90\text{dBm}) = 15\text{dB}$

# Simple Path Loss Model

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- Friis transmission equation

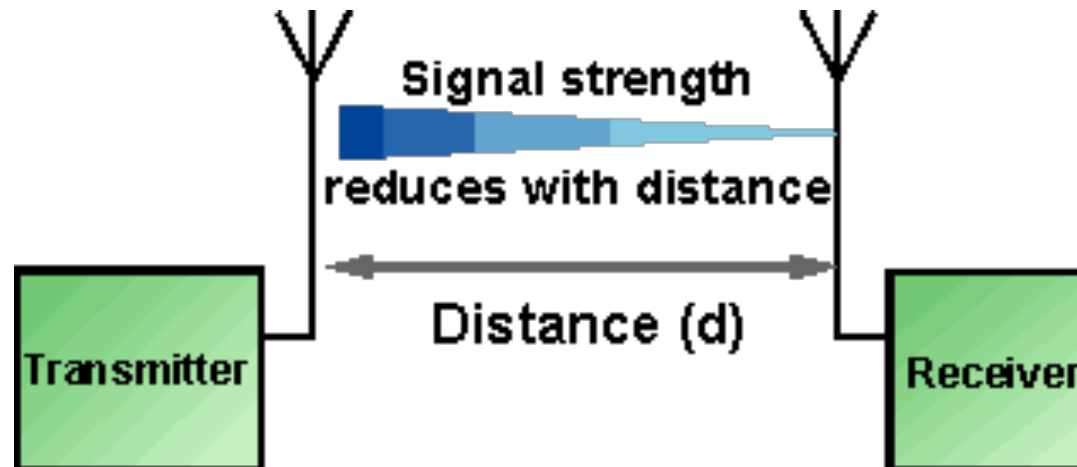
$$\frac{P_r}{P_t} = G_t G_r \left( \frac{\lambda}{4\pi d} \right)^2$$

- $G_t$ : gain of the transmit antenna
- $G_r$ : gain of the receive antenna
- $d$ : distance between the transmitter and receiver
- $\lambda$ : wavelength (= light speed/frequency)

# Free-Space Path Loss model

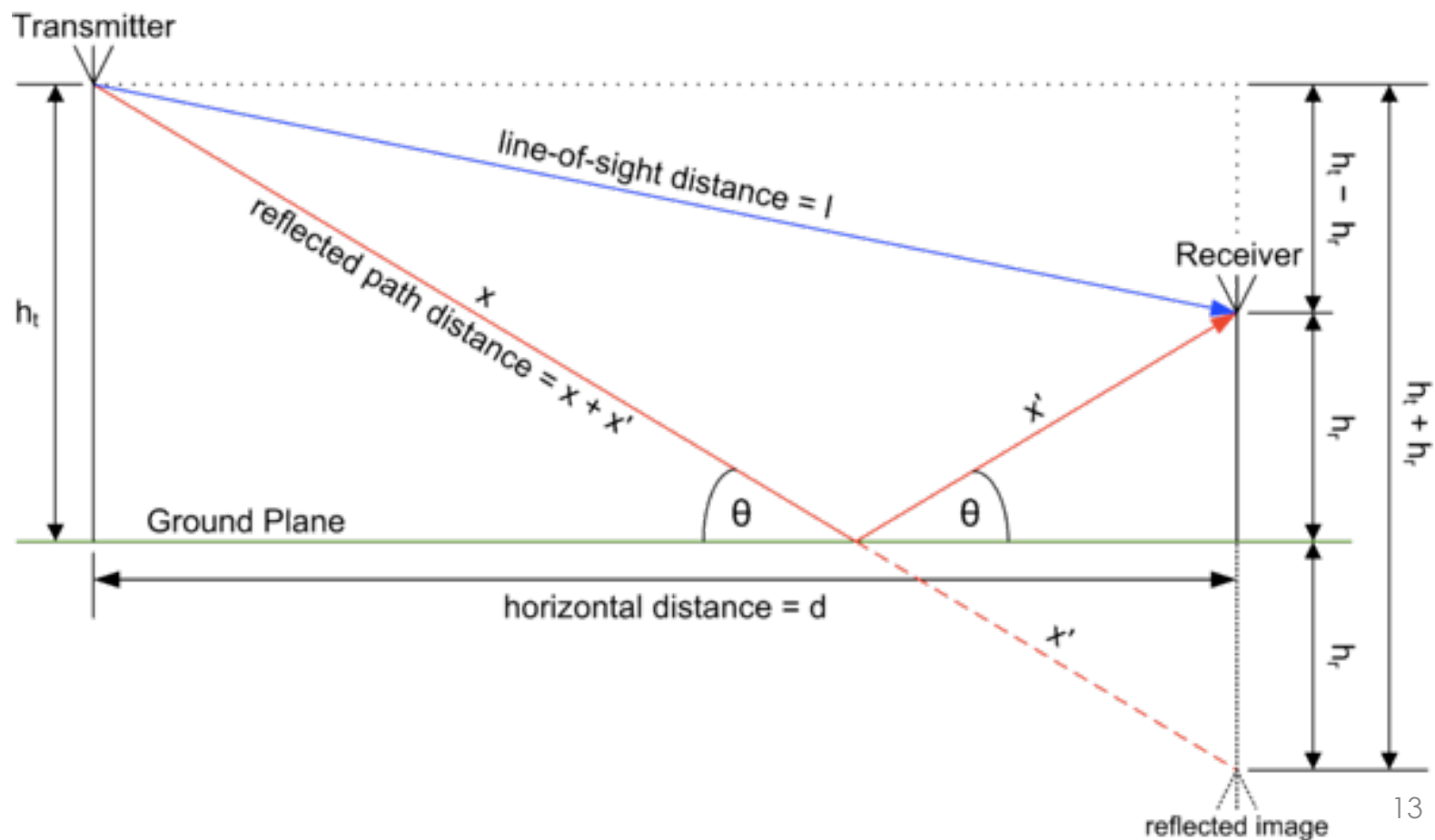
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- Only consider the loss resulting from the line-of-sight (LOS) path



# Two-ray Ground-Reflection Model

- Only consider the losses from the LOS path and the path reflected by the ground



# Outline

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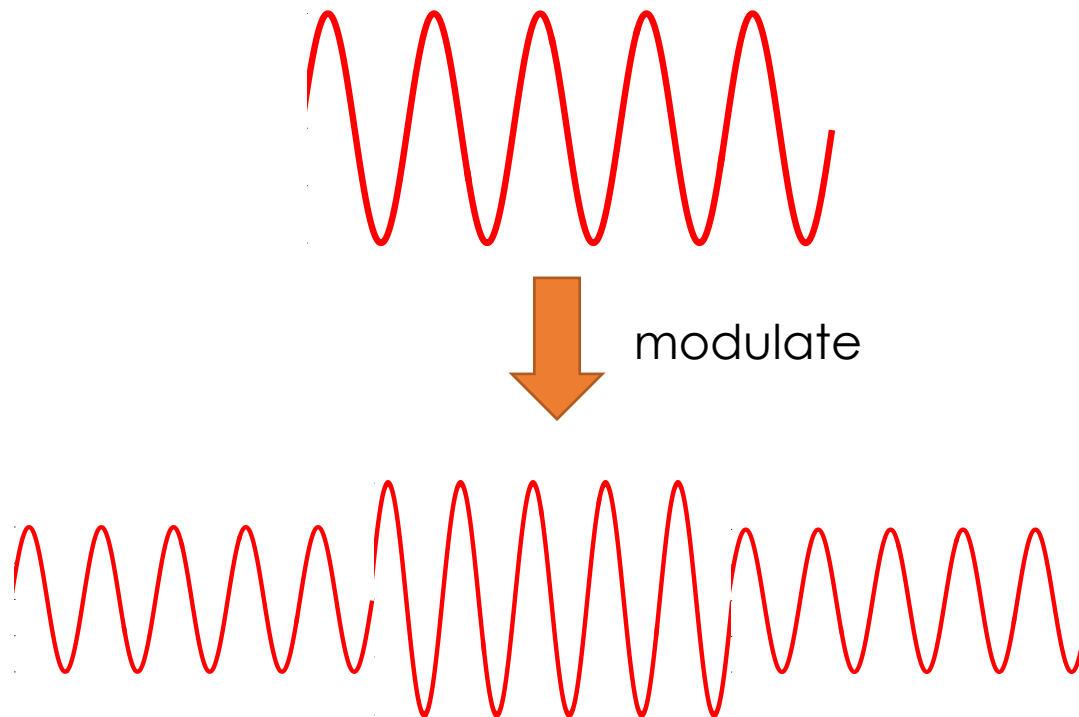
- SNR and capacity
- Channel fading and path loss
- **Modulation and coding scheme**
- Rate adaptation
- Wireless multicasting

# Modulation

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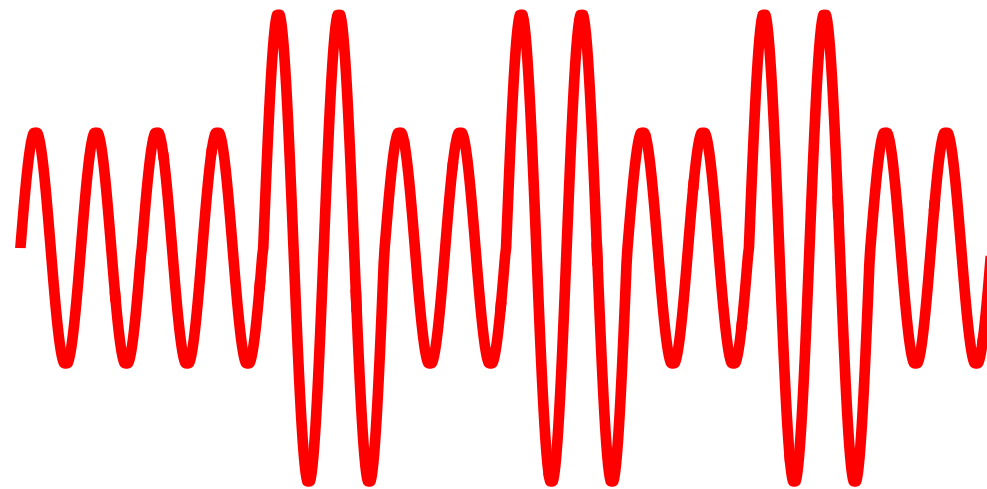
*From Wikipedia:*

*The process of varying one or more properties of a periodic [waveform](#) with a modulating signal that typically contains information to be transmitted.*



# Example 1

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= bit-stream?

(a) 10110011

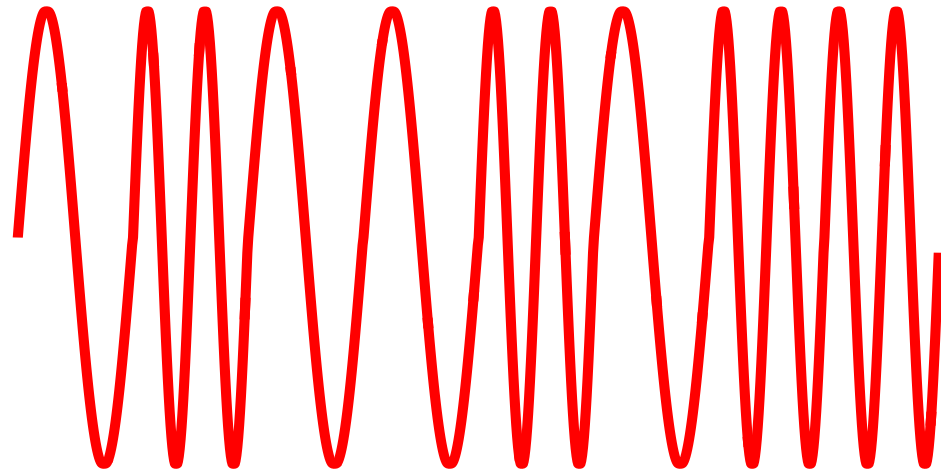
(b) 00101010

(c) 10010101



# Example 2

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= bit-stream?

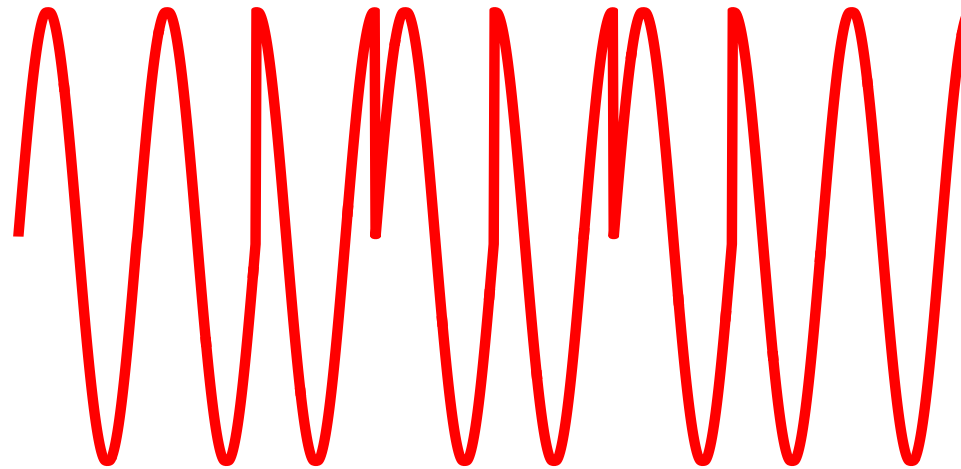
(a) 01001011

(b) 00101011

(c) 11110100

# Example 3

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= bit-stream?

(a) 11010100

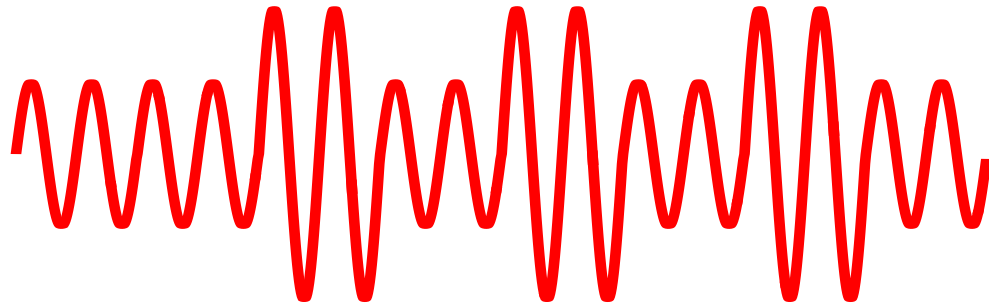
(b) 00101011

(c) 01010011

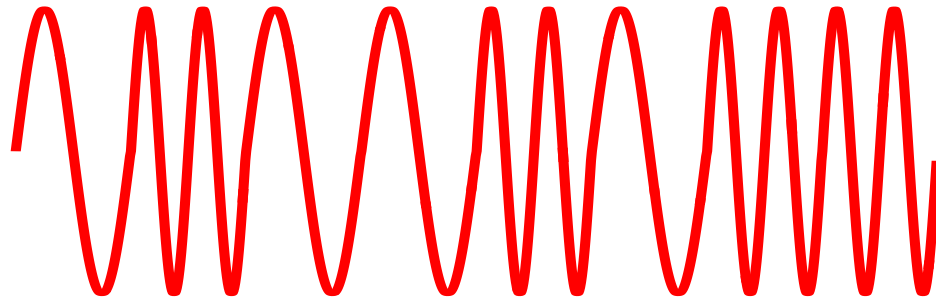
(d) 11010100 or  
00101011

# Types of Modulation

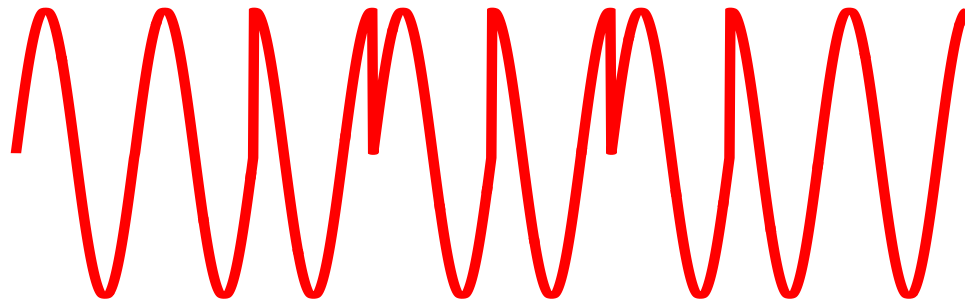
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Amplitude  
ASK



Frequency  
FSK

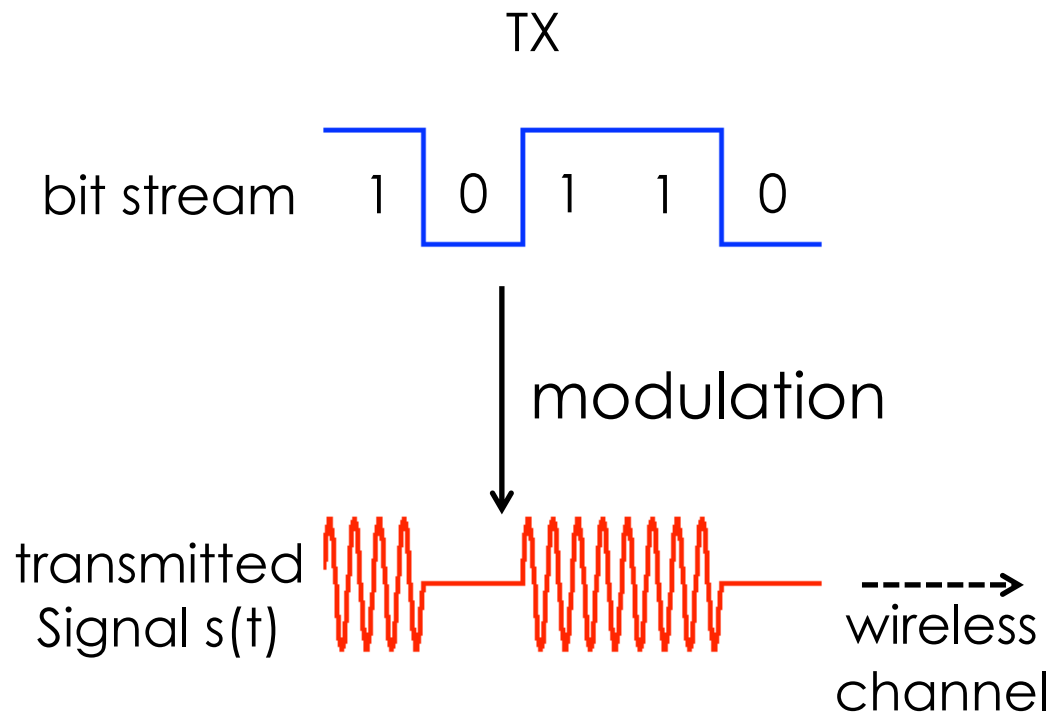


Phase  
PSK

# Modulation

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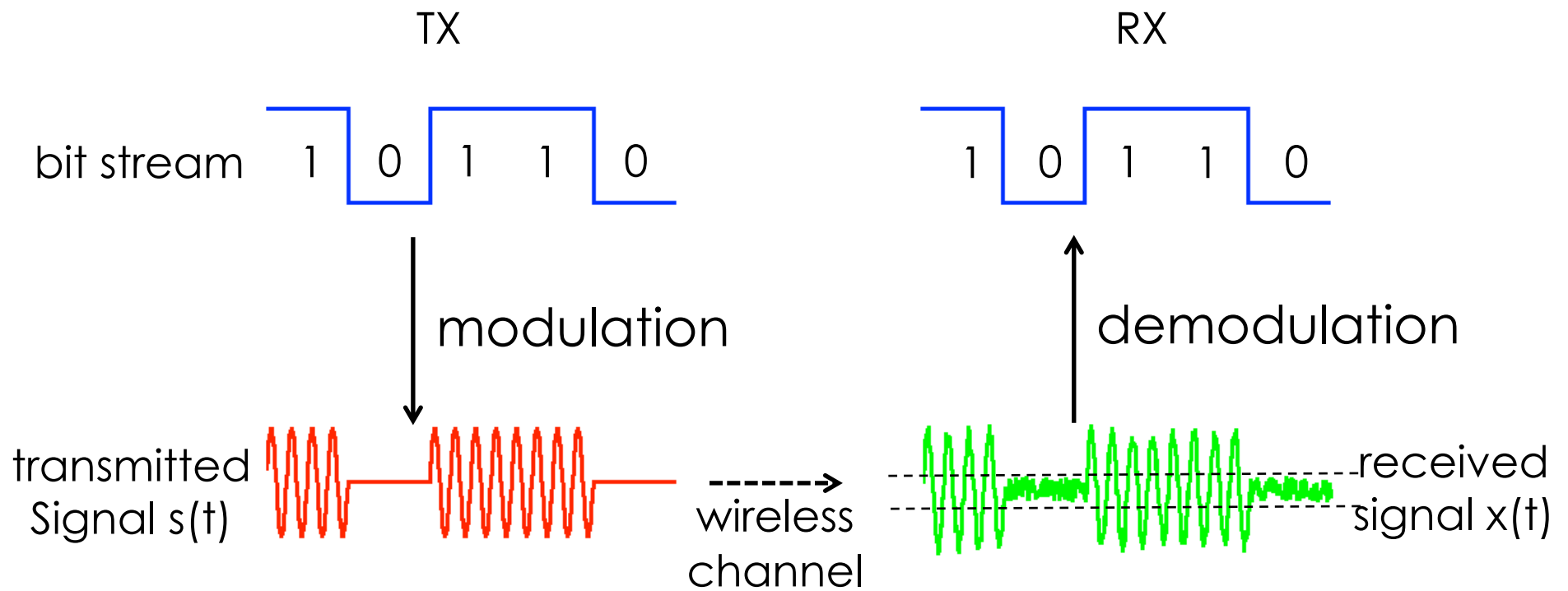
- Map bits to signals



# Demodulation

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- Map signals to bits



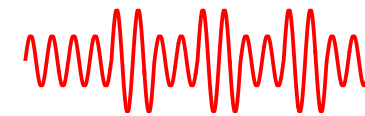
# Types of Modulation

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$$s(t) = A \cos(2\pi f_c t + \phi)$$

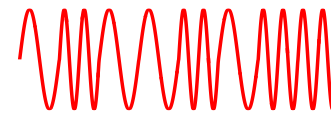
- *Amplitude*

- M-ASK: Amplitude Shift Keying



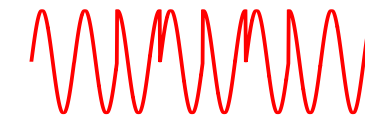
- *Frequency*

- M-FSK: Frequency Shift Keying



- *Phase*

- M-PSK: Phase Shift Keying

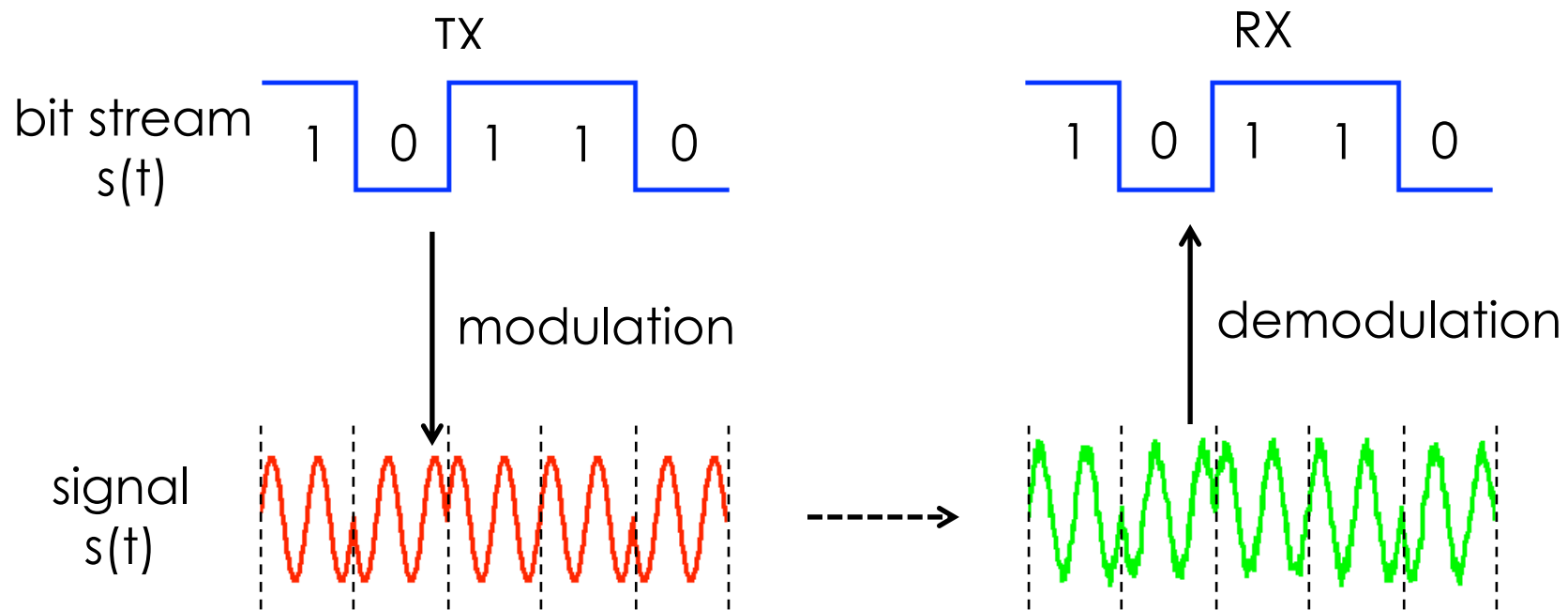


- *Amplitude* + *Phase*

- M-QAM: Quadrature Amplitude Modulation

# Phase Shift Keying (PSK)

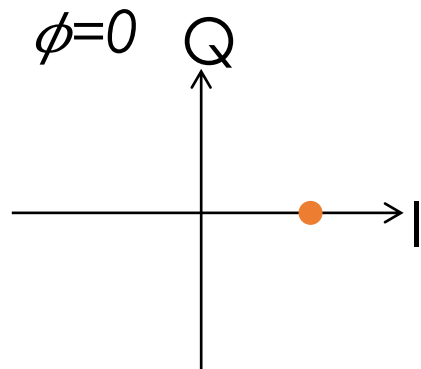
- A bit stream is encoded in the **phase** of the transmitted signal
- Simplest form: **Binary PSK (BPSK)**
  - '1'  $\rightarrow \phi=0$ , '0'  $\rightarrow \phi=\pi$



# Constellation Points for BPSK

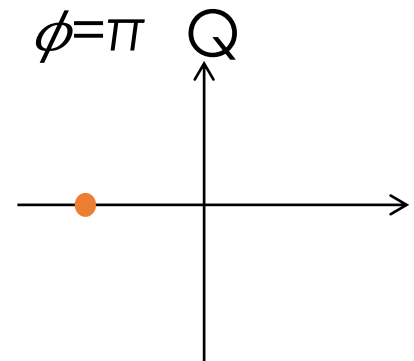
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- '1'  $\rightarrow \phi=0$
- $\cos(2\pi f_c t + 0)$   
= **cos(0)** $\cos(2\pi f_c t)$  -  
**sin(0)** $\sin(2\pi f_c t)$   
= **s<sub>I</sub>** $\cos(2\pi f_c t)$  - **s<sub>Q</sub>** $\sin(2\pi f_c t)$



$$(s_I, s_Q) = (1, 0)$$
$$'1' \rightarrow 1 + 0i$$

- '0'  $\rightarrow \phi=\pi$
- $\cos(2\pi f_c t + \pi)$   
= **cos(pi)** $\cos(2\pi f_c t)$  -  
**sin(pi)** $\sin(2\pi f_c t)$   
= **s<sub>I</sub>** $\cos(2\pi f_c t)$  - **s<sub>Q</sub>** $\sin(2\pi f_c t)$

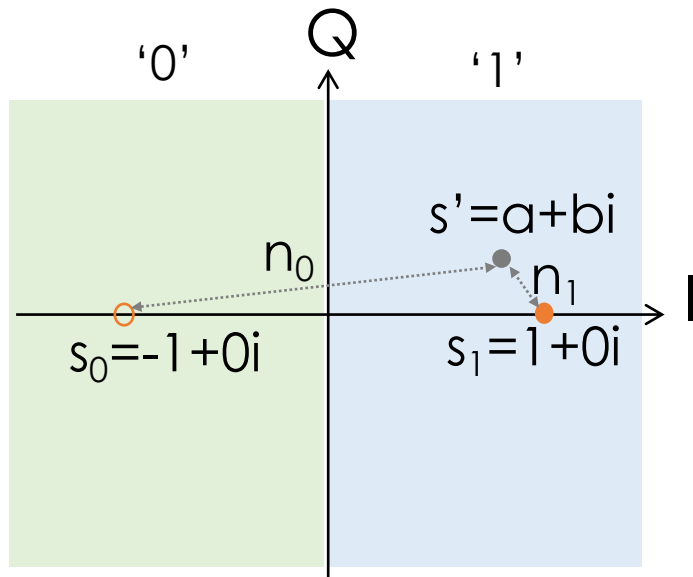


$$(s_I, s_Q) = (-1, 0)$$
$$'0' \rightarrow -1 + 0i$$



# Demodulate BPSK

- Map to the closest constellation point
- Quantitative measure of the distance between the received signal  $s'$  and any possible signal  $s$ 
  - Find  $|s'-s|$  in the I-Q plane

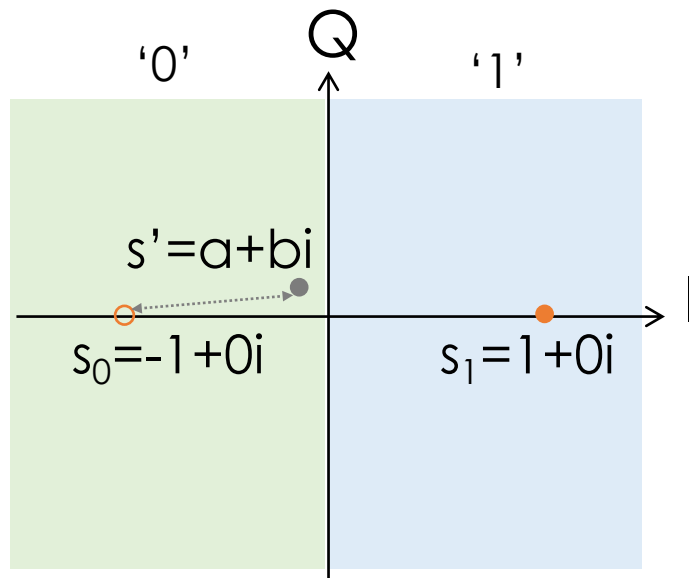


$$n_1 = |s' - s_1| = |s' - (1 + 0i)|$$
$$n_0 = |s' - s_0| = |s' - (-1 + 0i)|$$

since  $n_1 < n_0$ , map  $s'$  to  $(1 + 0i) \rightarrow '1'$

# Demodulate BPSK

- Decoding error
  - When the received signal is mapped to an incorrect symbol (constellation point) due to a large error
- Symbol error rate
  - $P(\text{mapping to a symbol } s_j, j \neq i \mid s_i \text{ is sent})$



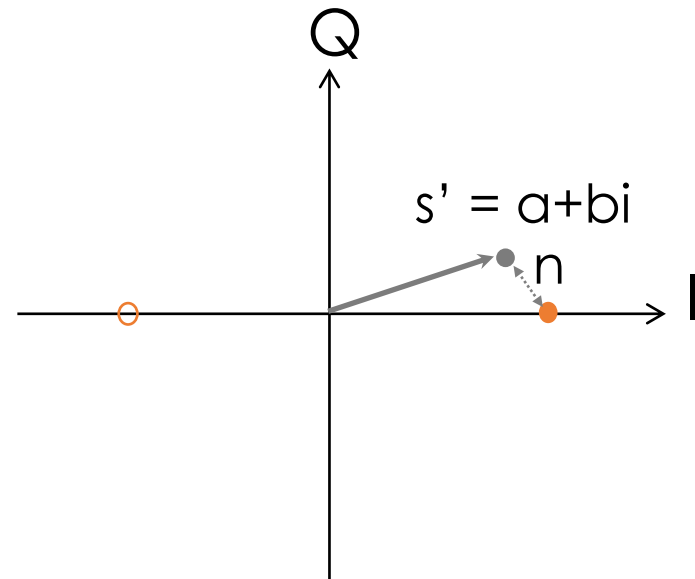
Given the transmitted symbol  $s_1$   
→ incorrectly map  $s'$  to  $s_0 = (-1 + 0) \rightarrow$  '0', when the error is too large

# SNR of BPSK

- SNR: Signal-to-Noise Ratio

$$SNR = \frac{|s|^2}{n^2} = \frac{|s|^2}{|s' - s|^2}$$
$$= \frac{|1 + 0i|^2}{|(a + bi) - (1 + 0i)|^2}$$

$$SNR_{dB} = 10 \log_{10}(SNR)$$



- Example:

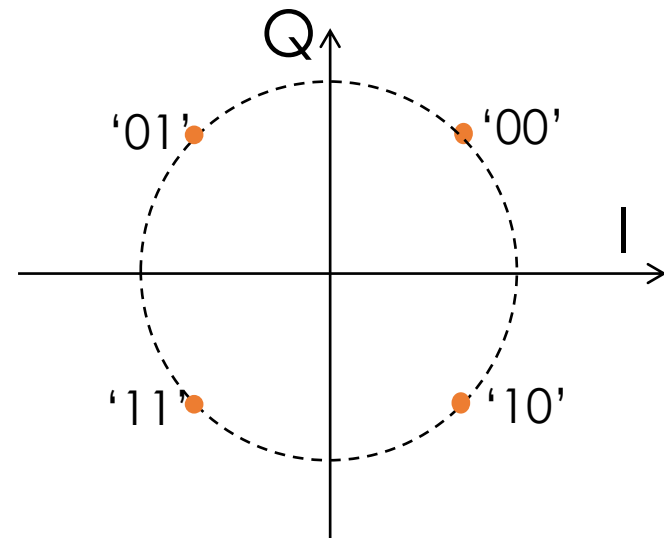
- Say Tx sends  $(1+0i)$  and Rx receives  $(1.1 - 0.01i)$
- SNR?

- Bit error rate:  $P_b = Q\left(\sqrt{\frac{E_b}{N_0}}\right)$

# Quadrature PSK (QPSK)

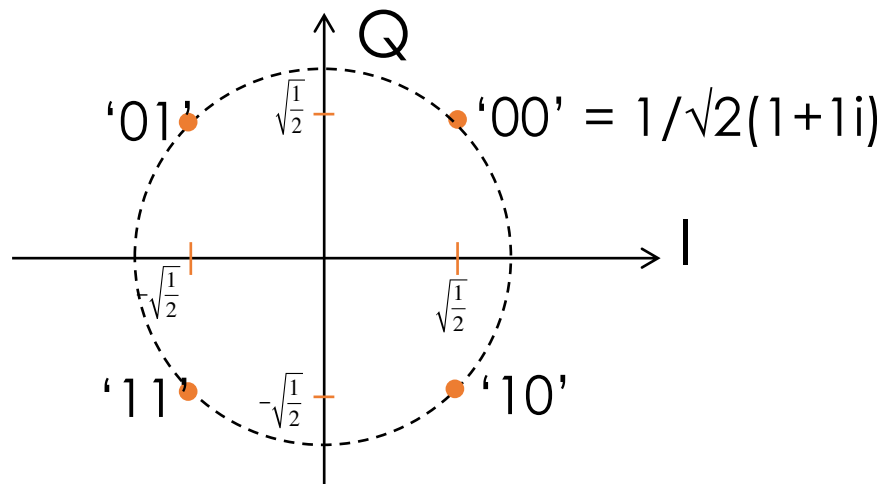
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- Use 2 degrees of freedom in I-Q plane
- Represent **two bits** as **a constellation point**
  - Rotate the constellations by  $\pi/2$
  - Demodulation by mapping the received signal to the closest constellation point
  - Double the bit-rate
- No free lunch:
  - Higher error probability (Why?)



# Quadrature PSK (QPSK)

- Maximum power is bounded
  - Amplitude of each constellation point should still be 1



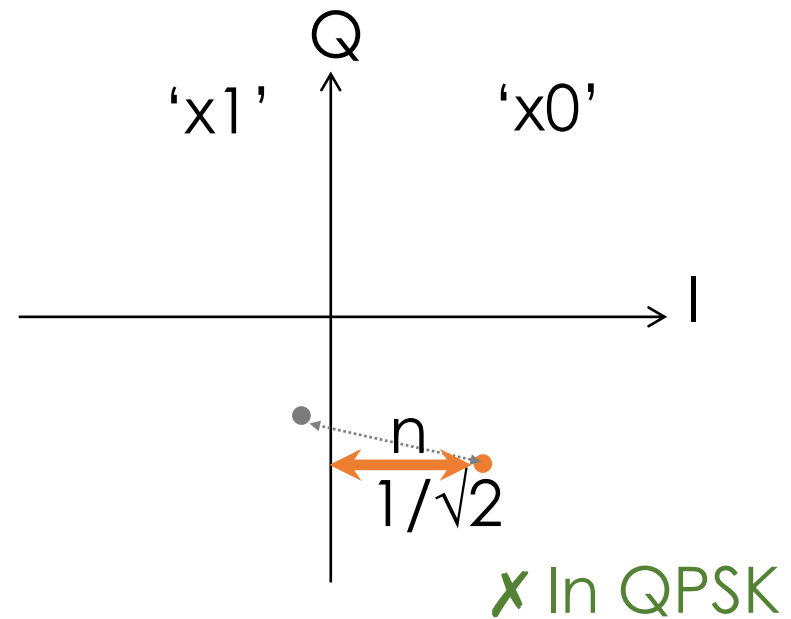
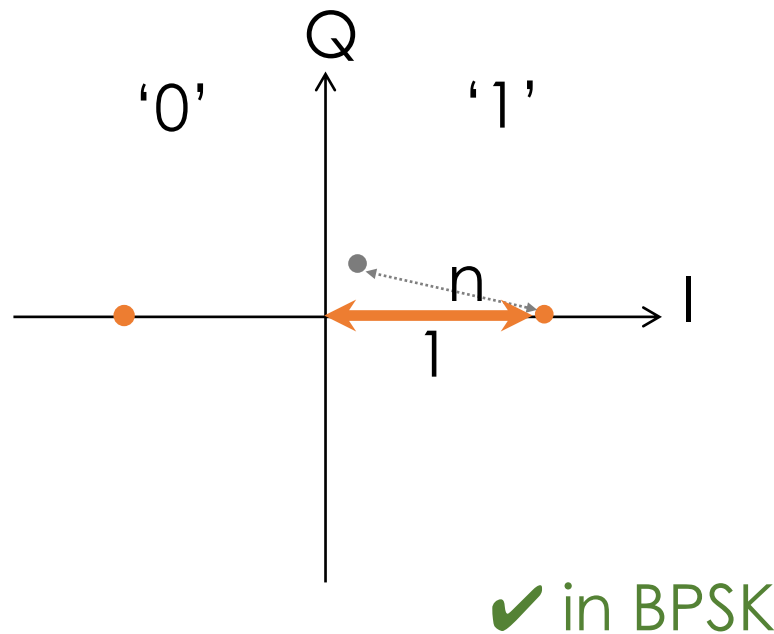
Bits	Symbols
'00'	$1/\sqrt{2}+1/\sqrt{2}i$
'01'	$-1/\sqrt{2}+1/\sqrt{2}i$
'10'	$1/\sqrt{2}-1/\sqrt{2}i$
'11'	$-1/\sqrt{2}-1/\sqrt{2}i$

- Bit error rate:

$$P_b = 2Q \left( \sqrt{\frac{2E_b}{N_0}} \right) \left[ 1 - \frac{1}{2} Q \sqrt{\frac{2E_b}{N_0}} \right]$$

# Higher Error Probability in QPSK

- For a particular error  $n$ , the symbol could be decoded correctly in BPSK, but not in QPSK
  - Why? Each sample only gets half power



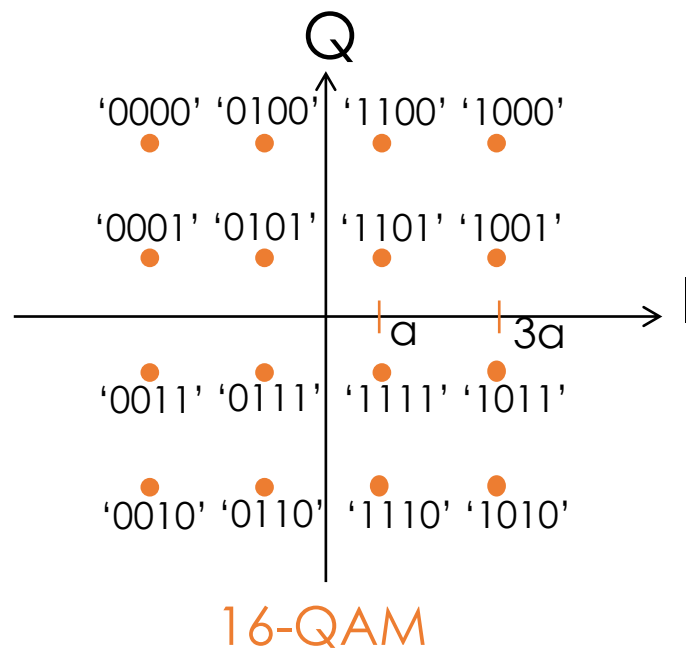
# Trade-off between Rate and SER

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- Trade-off between the data rate and the symbol error rate
- Denser constellation points
  - More bits encoded in each symbol
  - Higher data rate
- Denser constellation points
  - Smaller distance between any two points
  - Higher decoding error probability

# Quadrature Amplitude Modulation

- Change both amplitude and phase
- $s(t) = A \cos(2\pi f_c t + \phi)$



Bits	Symbols
------	---------

'1000'	$s_1 = 3a + 3ai$
--------	------------------

'1001'	$s_2 = 3a + ai$
--------	-----------------

'1100'	$s_3 = a + 3ai$
--------	-----------------

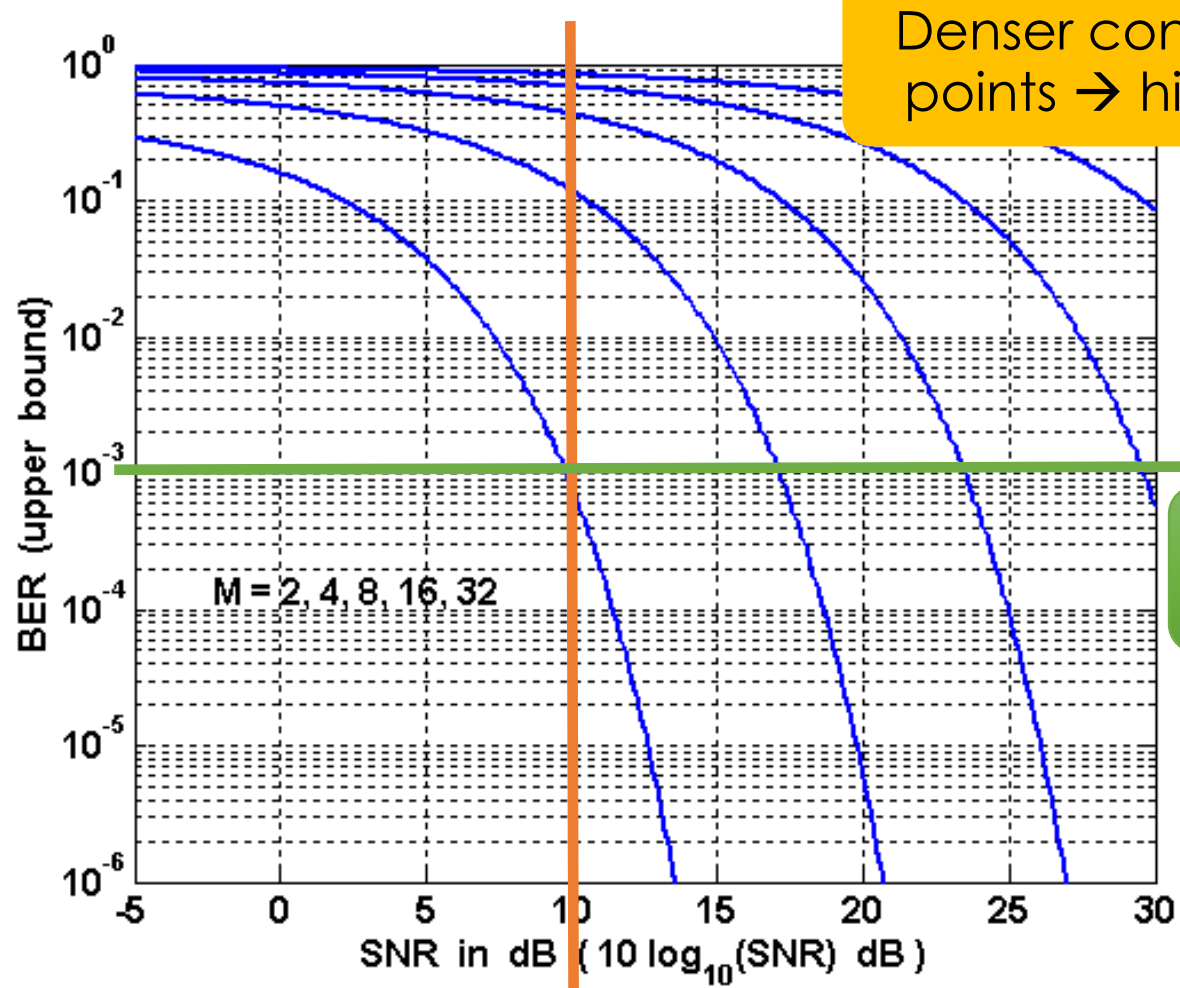
'1101'	$s_4 = a + ai$
--------	----------------

expected power:  $E[|s_i|^2] = 1$

- 64-QAM: 64 constellation points, each with 8 bits



# M-QAM BER versus SNR



# Modulation in 802.11

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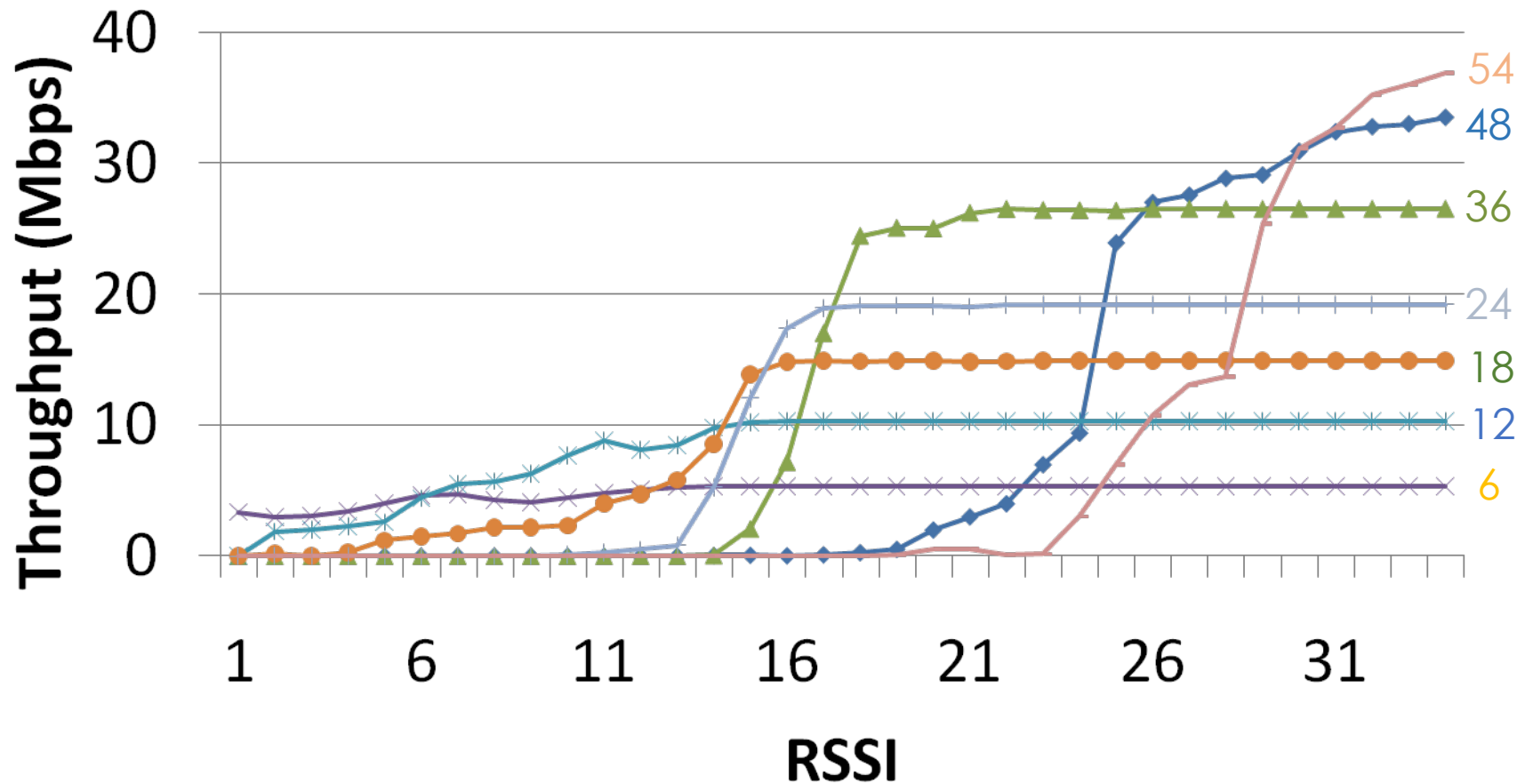
- 802.11a
  - 6 mb/s: BPSK +  $\frac{1}{2}$  code rate
  - 9 mb/s: BPSK +  $\frac{3}{4}$  code rate
  - 12 mb/s: QPSK +  $\frac{1}{2}$  code rate
  - 18 mb/s: QPSK +  $\frac{3}{4}$  code rate
  - 24 mb/s: 16-QAM +  $\frac{1}{2}$  code rate
  - 36 mb/s: 16-QAM +  $\frac{3}{4}$  code rate
  - 48 mb/s: 64-QAM +  $\frac{2}{3}$  code rate
  - 54 mb/s: 64-QAM +  $\frac{3}{4}$  code rate
- FEC (forward error correction)
  - k/n: k-bits useful information among n-bits of data
  - Decodable if any k bits among n transmitted bits are correct

# Outline

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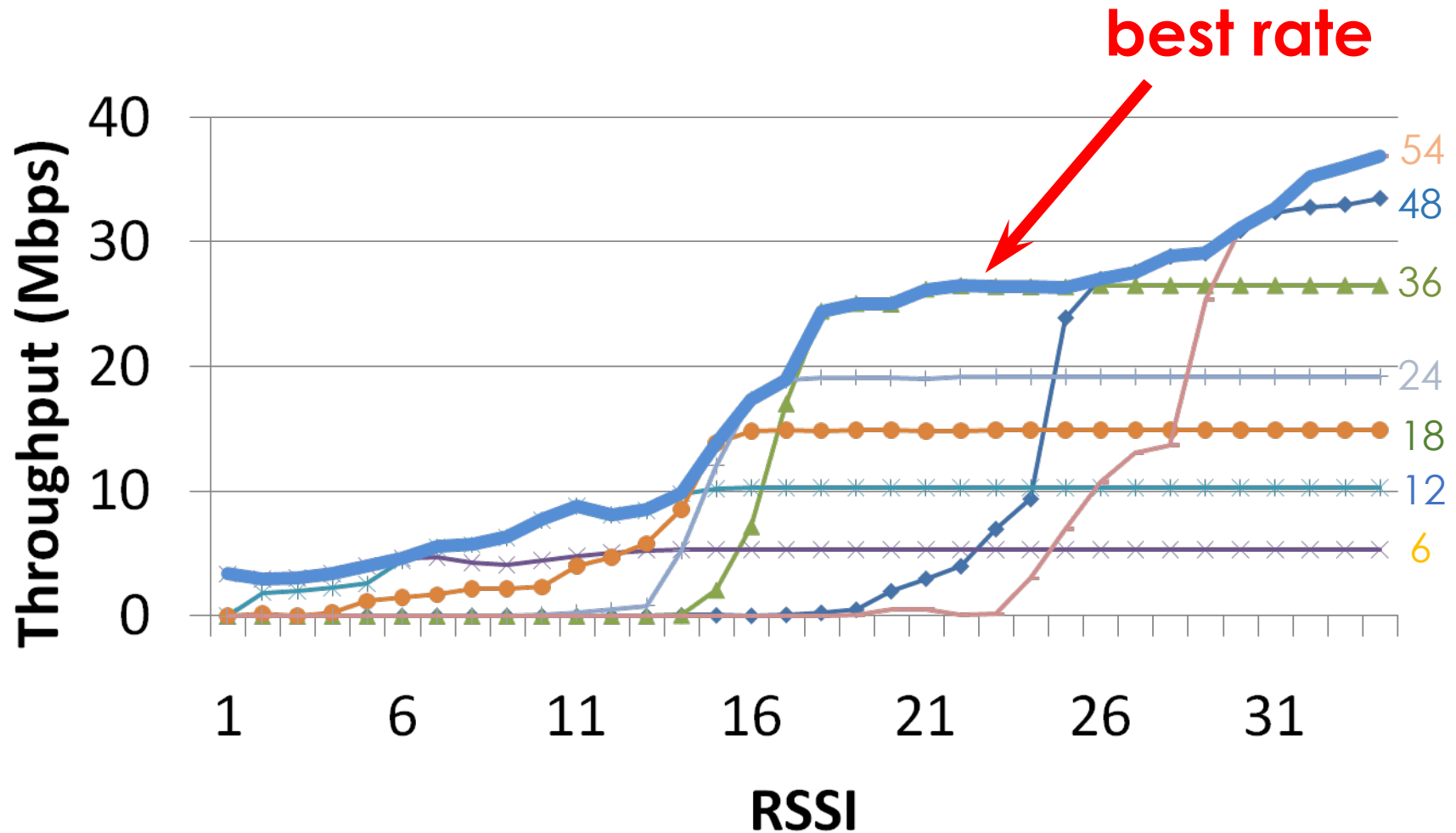
- SNR and capacity
- Channel fading and path loss
- Modulation and coding scheme
- **Rate adaptation**
- Wireless multicasting

# Bit-Rate Selection



$$\text{throughput} = (1 - \text{PER}_{r, \text{SNR}}) * r = (1 - \text{BER}_{r, \text{SNR}})^N * r$$
$$r^* = \arg \max \text{throughput}_r$$

# Bit-Rate Selection



Adapt bit-rate to dynamic RSSI

# Difficulties with Rate Adaptation

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- Channel quality changes very quickly
  - Especially when the device is moving
- Can't tell the difference between
  - poor channel quality due to **noise/interference/collision** (high | noise | )
  - poor channel quality due to **long distance** (low | signal | )

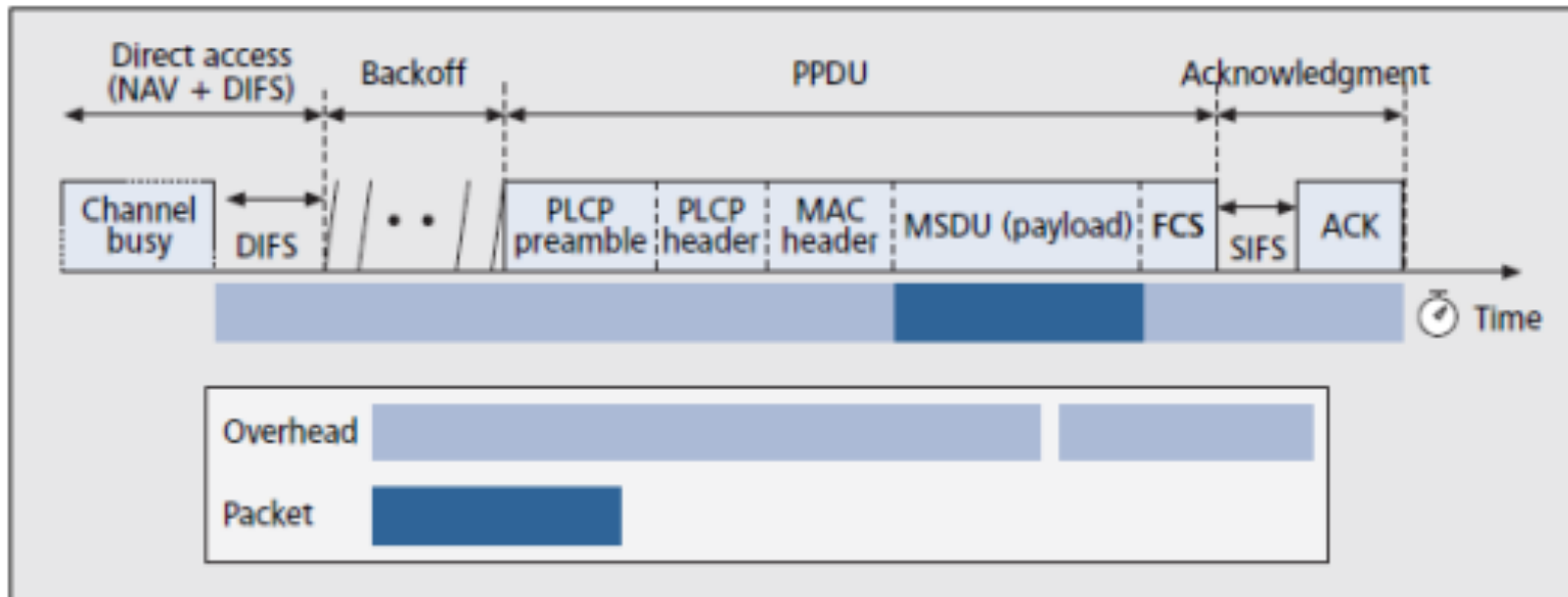
Ideally, we want to decrease the rate due to low signal strength, but not interference/collisions

# Types of Auto-Rate Adaptation

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	Transmitter-based	Receiver-Based
SNR-based		RBAR, OAR, ESNR
ACK-based	ARF, AARF, ONOE	
Throughput-based	<b>SampleRate, RRAA</b>	
Partial packet		ZipTx
Soft information		SoftRate

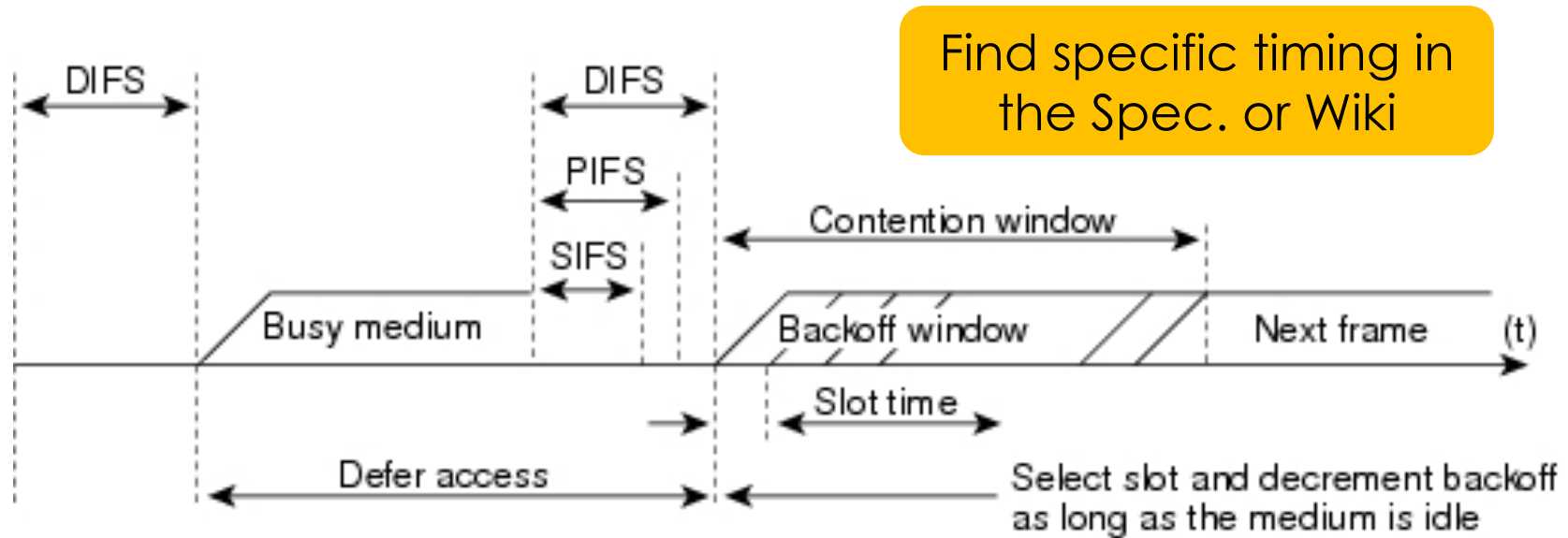
# 802.11 MAC



- Start contention after the channel **keeps idle for DIFS**
- Avoid collisions via **random backoff**
- AP responds ACK if the frame is delivered correctly (i.e., passing the CRC check) → No NACK
- **Retransmit** the frame until the retry limit is reached



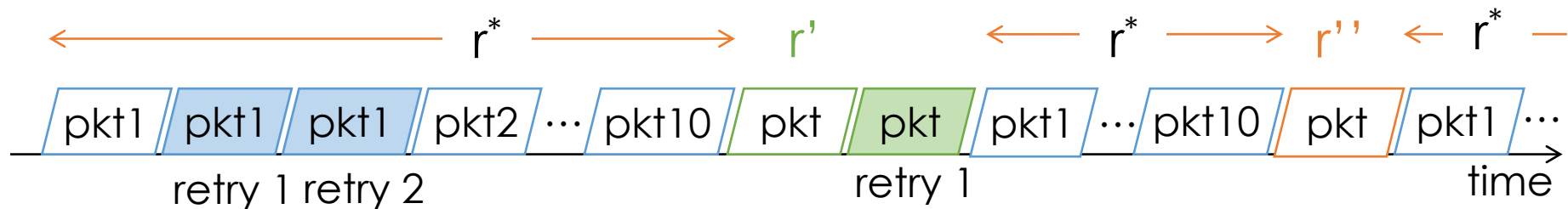
# Prioritized Interframe Spacing



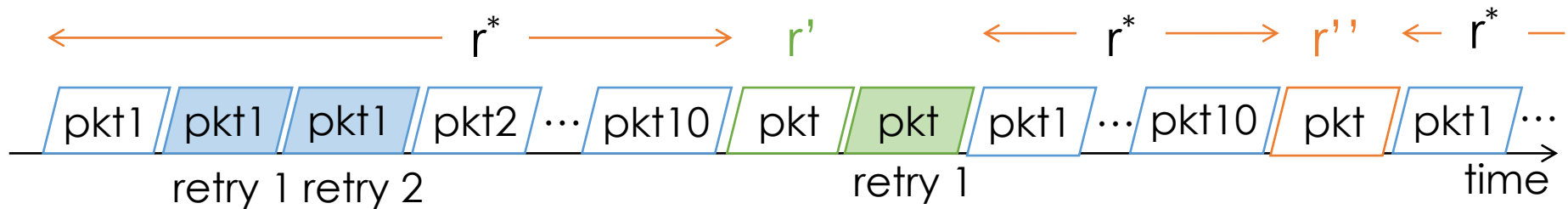
- Latency:  $SIFS < PIFS < DIFS$   
Priority:  $SIFS > PIFS > DIFS$
- SIFS (Short interframe space): control frames, e.g., ACK and CTS
- PIFS (PCF interframe space): CF-Poll
- DIFS (DCF interframe space): data frame

# SampleRate – Tx-based Adaptation

- Default in Linux
- Periodically send packets at a **randomly-sampled bit-rate other than the current bit-rate**
  - Let  $r^*$  be the current best rate
  - After sending 10 packets at the best rate, send a packet at a **randomly-sampled** rate
  - Estimate the achievable throughput of the **sampled** rates



# SampleRate – Throughput Estimation



- How to estimate the effective throughput of a rate?
  - Calculate the transmission time of a L-bit packet
  - Consider packet length ( $l$ ), bit-rate ( $r$ ), number of retries ( $n$ ), backoff time

$$T_{tx}(r, n, l) = T_{DIFS} + T_{back\ off}(n) + (n + 1)(T_{SIFS} + T_{ACK} + T_{header} + l/r)$$

- Select the rate that has the smallest measured average transmission time to deliver a L-bit packet

$$r^* = \min_r T_{tx}(r, n, L)$$

# SampleRate

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- Do not sample the rates that
  - Have failed four successive times
  - Are unlikely to be better than the current one
- Is thought of the most efficient scheme for **static environments**
  - SNR, and thereby BER and best rate, do not change rapidly over time
- Waste channel time for sampling if the channel is very stable

# Outline

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- SNR and capacity
- Channel fading and path loss
- Modulation and coding scheme
- Rate adaptation
- **Wireless multicasting**

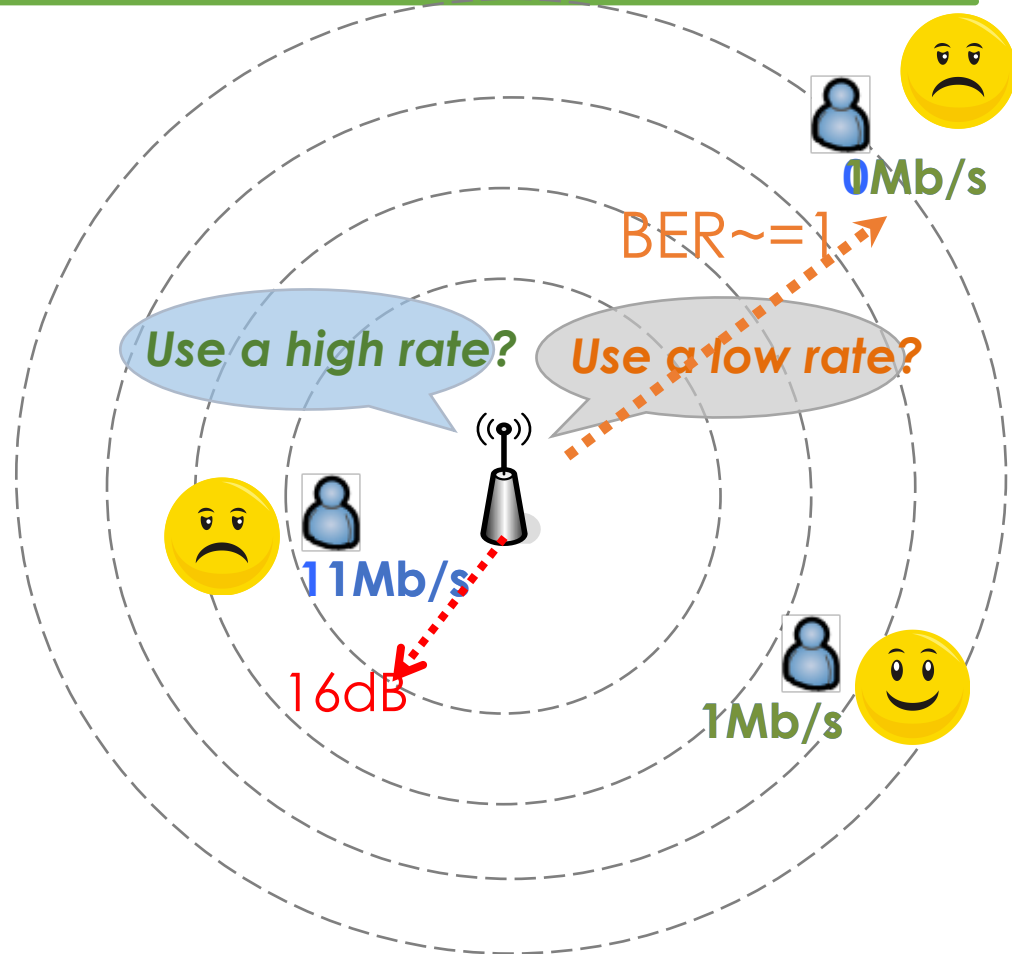
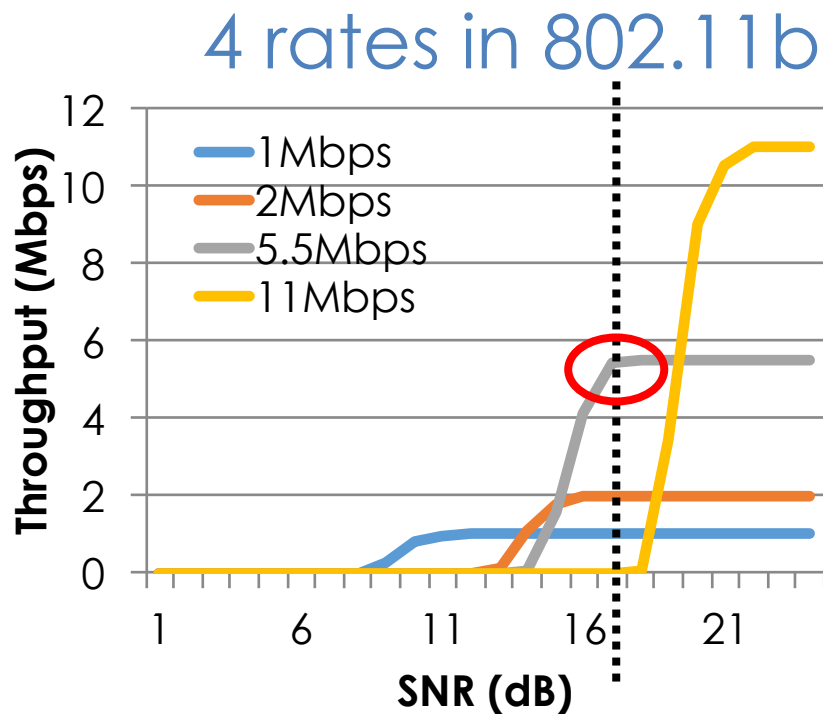
# Wireless Multicast

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- Achieve a **higher throughput**
- Packets are **randomly lost** on a noisy wireless channel
- Link reliability decreases with the **link distance**
- Different receivers may lose different packets

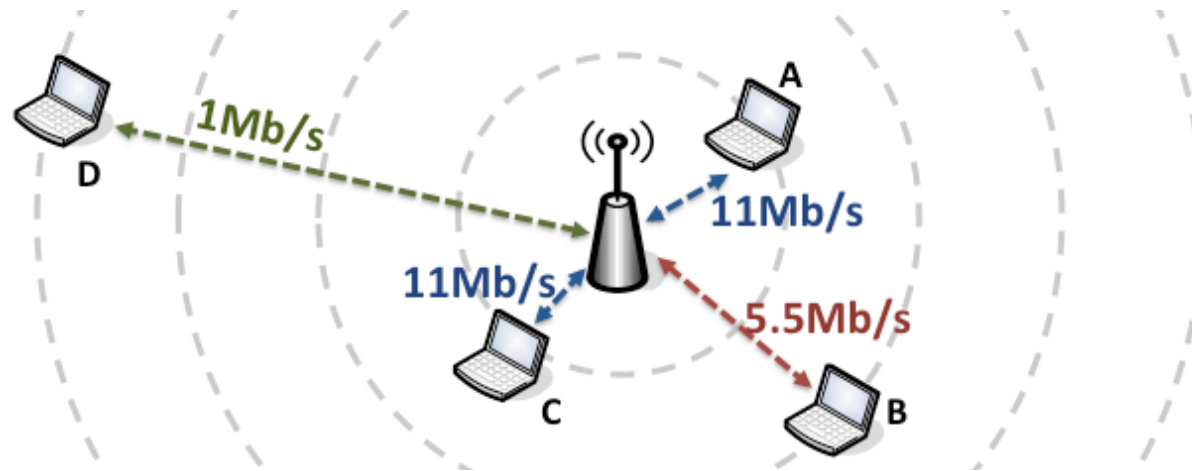
# Heterogeneous Channel Conditions



Higher rates provide a higher throughput, but a shorter coverage range

# Rate Adaptation for Multicast

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- Why it is difficult?
  - Can only assign a single rate to each packet
  - But the channel conditions of clients are different
- Possible Solutions
  - **For reliable transmission:** select the rate based on the worst node
  - **For non-reliable transmission:** provide clients heterogeneous throughput



# Reliable Multicast Protocol

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- Before rate adaptation, we should first ask:
  - How to efficiently collect ACK from multicast clients?
- Leader-based Protocol (LBP)
  - Select one of the receivers as the leader to reply ACK
  - **Leader**  
if receive successfully, send ACK  
otherwise, send NACK
  - **Others**  
if receive successfully, do nothing  
otherwise, send NACK
  - Retransmit if the AP receives any NACK

J. Kuri and S. Kaser, "Reliable Multicast in Multi-Access Wireless LANs,"  
IEEE INFOCOM, Mar. 1999.

# Rate Adaptation for Data Multicast

- Rate Adaptive Reliable Multicast (RAM)
  - Should pick the bit-rate based on the channel of the worst receiver
- Say we have three receivers A, B, and C
  - Each receiver feedbacks CTS at its optimal rate chosen based on its SNR
  - The AP detects the lowest rate by measuring the longest channel time occupied by CTS

