

Game Theory and Its Applications



Syllabus
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What is Game Theory?

- the study of mathematical models of strategic interaction between rational decision-makers.
- Which are in the field of game theory?

chess playing? **bidding?**
trade war? **buying a lottery?**
solving a puzzle? **bargaining?**
playing Sudoku? **forming an alliance?**

What's the difference?

- Whether your choice is good or not depends on other people's choice(s).
 - and vice versa



Interdependence

So What?

- ‘I can select a best choice considering all other people’s possible choices.’--- a belief
- Sometimes you have **no knowledge** of other people’s choices.
- Sometimes there are just **too many** possible choices to consider
- Sometimes everyone’s best choice (despite thoughtful) is **not the best** as a whole

**Let's take a look at a classic
example**

Prisoner's Dilemma

- Two gangsters (A and B) are arrested and imprisoned
- They are interrogated separately with no means of communicating with the other

A \ B	B stays silent	B betrays
A stays silent	-1 / -1	0 / -3
A betrays	0 / -3	-2 / -2

If you were Prisoner A ...

- What would be your choice?



		B	
		B stays silent	B betrays
A	A stays silent	-1 / -1	0 / -3
	A betrays	0 / -3	-2 / -2

Even if you don't know your partner's payoff...

- What would be your choice?



		B	
		B stays silent	B betrays
A	A stays silent	-1 / ?	-3 / ?
	A betrays	0 / ?	-2 / ?

If you consider Prisoner B ...

- What would be B's best choice?
- What will be your best response?
- Will B change her choice knowing your best response?
- Is there any better result?

		B	
		B stays silent	B betrays
A	A stays silent	-1 / -1	-3 / 0
	A betrays	0 / -3	-2 / -2

The table shows a 2x2 payoff matrix for Prisoner B. The rows represent Prisoner A's choices (stays silent or betrays) and the columns represent Prisoner B's choices (stays silent or betrays). The payoffs are given as (A's payoff, B's payoff). Red circles highlight B's best response in each row: a dashed circle around -1 in the top row and a solid circle around 0 in the bottom row. A solid red circle also highlights the 0 payoff in the bottom-left cell.

Why should I learn this?

- Traditionally, computer scientists play the role of a god, controlling and manipulating everything
- “Objects” (devices, resources, processes) do not have their **own interests**



The Game from a Computer Scientist's View

- You play the role of a god (omniscience)
- You **figure out** that 'stays silent' is the best choice for both prisoners
- You **instruct** each prisoner to take that strategy
- That's it
- If prisoners are self-interested, they may **deviate** from your instruction

		B	
		B stays silent	B betrays
A	A stays silent	-1 / -1	-3 / 0
	A betrays	0 / -3	-2 / -2

Game-Theoretic Approach

- design rules for game players (software agents)
- Players act in their own self-interest, as an indirect way to achieve society's economic goals (i.e., your system goal)
- For scenarios like
 - Task allocations among a fleet of robots, UAVs, or autonomous cars
 - Resource sharing among users, operators, or tenants
 - Clustering, grouping, or federation of a bunch of resource/task producers or consumers
 - Matching resource buyers with sellers or vice versa

Course Goals

- Game theory as an **analytic model**
 - to **model** your problem (but you solve it by another means)
- Game theory for **mechanism design**
 - to **solve** your problem in a decentralized and autonomous way
- Learning some well-known **mechanism designs**
- Solving games

So this course is **not** to ...

- study how to design a fancy computer game
 - You should courses like “3D Game Programming” (by Prof. Sai-Keung Wong)
- (in most of the time) study how to design a computer program to win a game (e.g., Go and Chess)
 - You should take “Theory of Computer Games” (by Prof. I-Chen Wu)

Compared with other Game Theory courses

- This course offers a **broader coverage**
 - It covers non-cooperative game, coalition game, matching, auction and related examples in CS/commun./networks
 - Many other courses cover only the first two topics
- This course **does not** cover application of Game theory to economics, politics, and biography
- This course minimizes the use of math. formulas
 - focus on concepts rather than math.

Criticisms of Game Theory

- They say: people are **not** always rational or self-interested
 - people may show mercy or tend to cooperate
 - Particularly in making economic or political decisions
- **Not a problem** at all in our case: we consider software agents, not human being

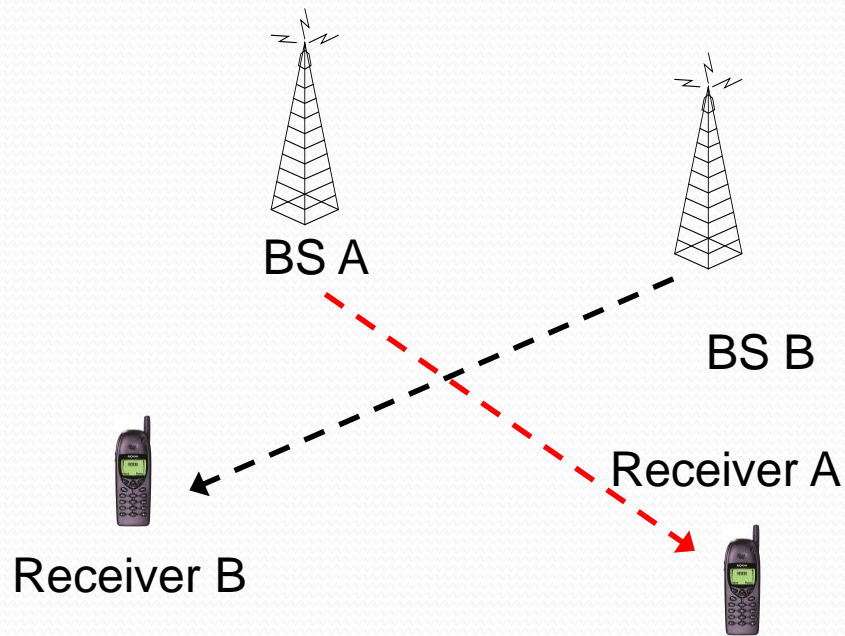
Course Goal One: Help Us Analyze

- Game theory as an **analytic model**
 - To predict what will happen next
 - To see if the interactions among players can be stable
 - To see whether we can make an improvement (if any)
 - primary concerns of Economists

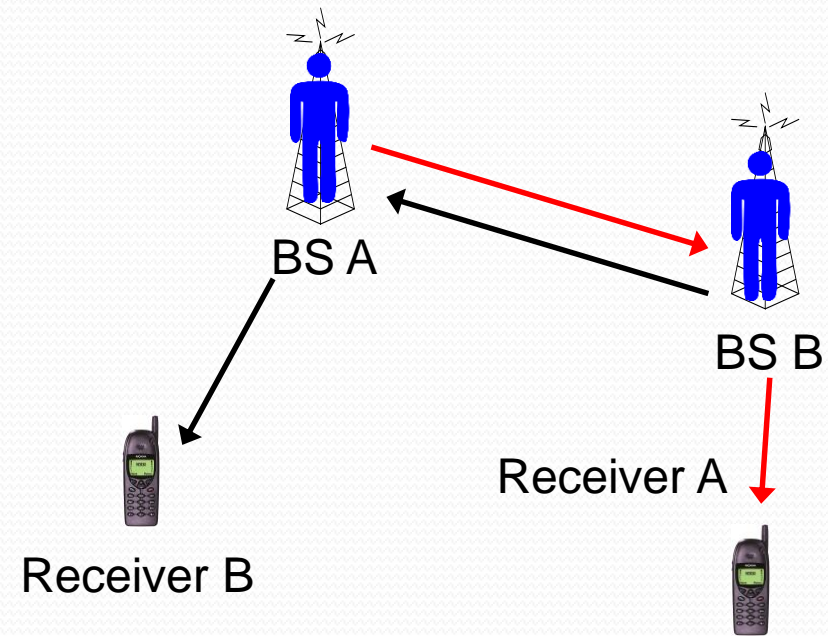


Example: Wireless Relay System

- Will a BS relay signal for the other?
- Can we motivate cooperation?



Direct Transmission



Relay Transmission

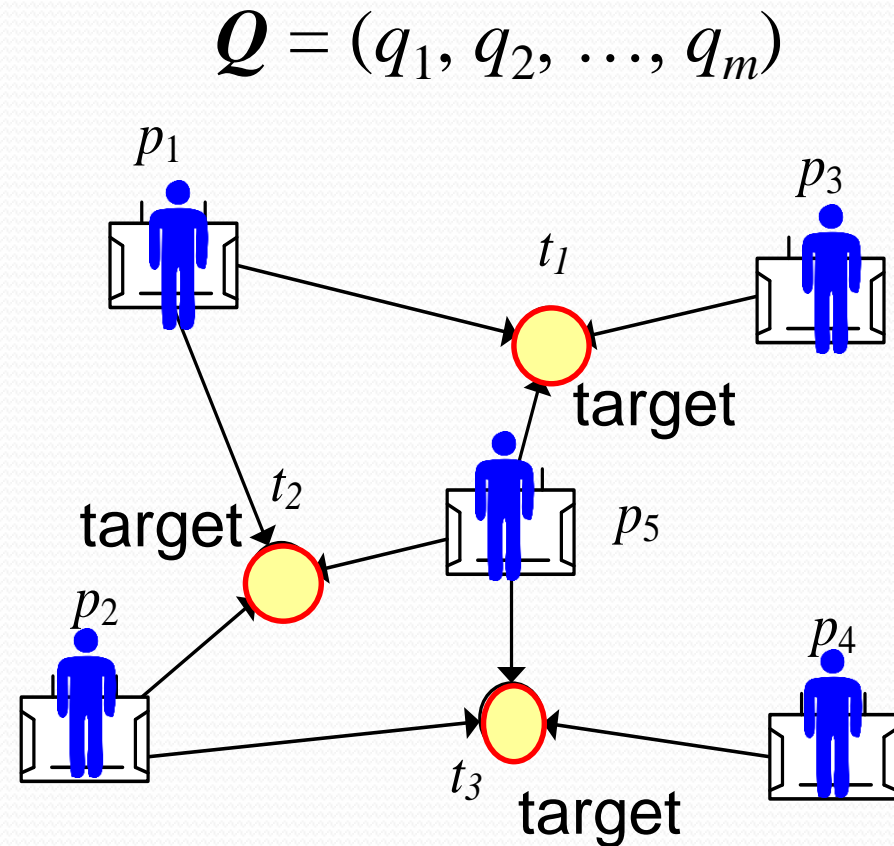
Course Goal Two: Help Us Design

- Game theory for **mechanism design**
 - To achieve a system goal via incentive-compatible rules
 - Design game rules for selfish yet rational players
 - yet achieve system goal
 - Decentralized, autonomous, adaptive, self-stabilizing, self-optimizing
 - main focus of computer scientist



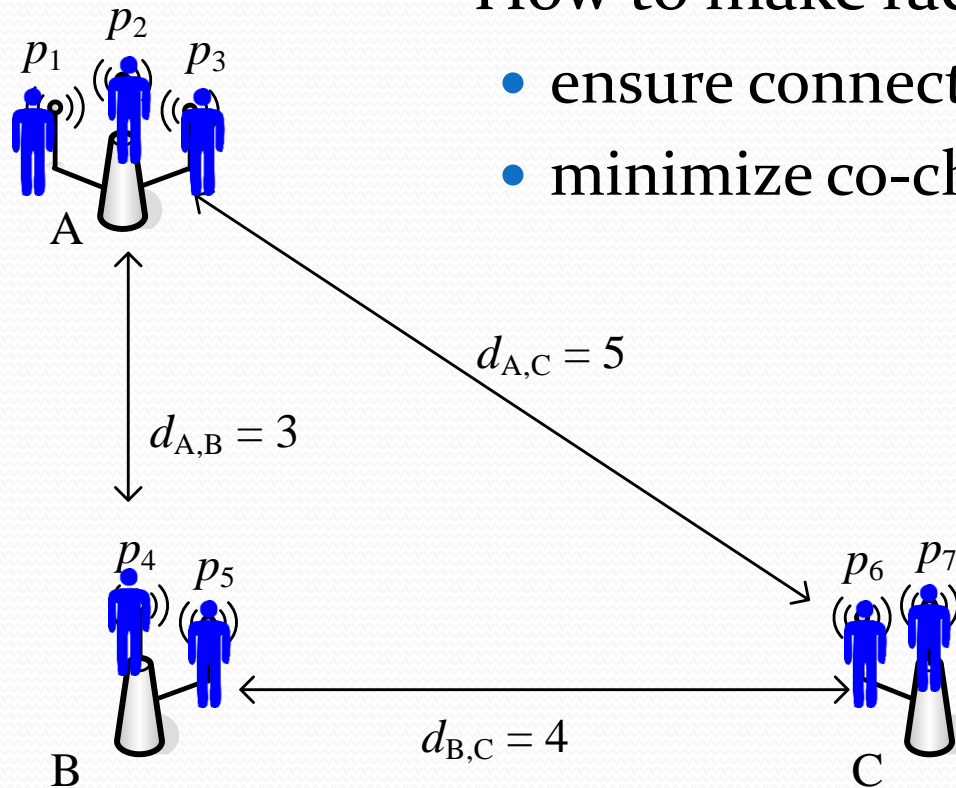
Example: Sensor Coverage

- n sensors are densely deployed to monitor m targets
- Target j must be covered by q_j sensors
- How to motivate sensors (game players) to meet coverage requirement while turning off sensors as many as possible?



Example: Channel Selection

- How to make radios select channels to
 - ensure connectivity
 - minimize co-channel interference



Course Goal Three: Help Us Know

- Learn some well-known **mechanism designs**
 - Auction
 - Matching
- with system goals
 - Pareto optimality
 - stability
 - social welfare



Example: Combinatorial Auctions

- How to select the set of winning bidders to maximize social welfare?
- How to enforce truthful bidding (bid indicates valuation)?

bidder	P1	P2	P3	P4	P5
valuation	\$63	\$54	\$93	\$70	\$28
bundle	{A,C,D}	{A,B,C}	{B,D,E}	{D,E}	{A,C}
bid					

A



B



C



D



E

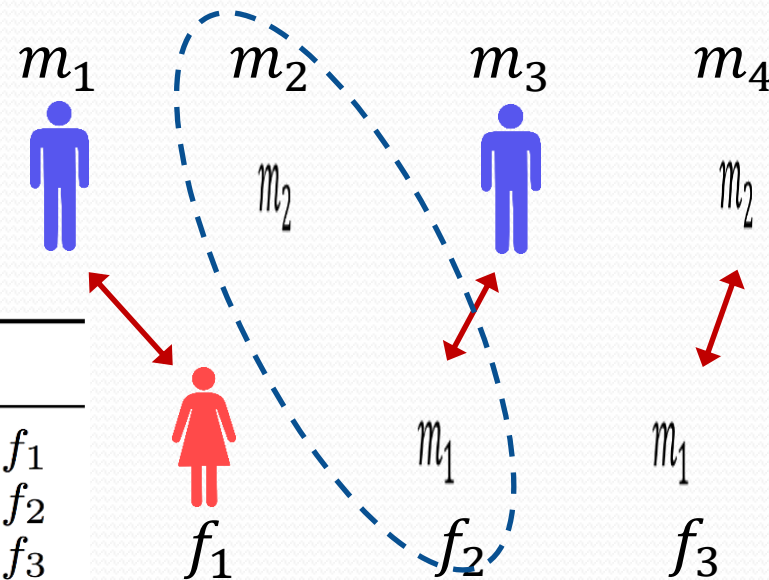


Example: Matching

- How to match females with males so that
 - no pair wants to deviate from the result?
 - no pair can be better off without hurting any others?

Male	Preference
m_1	$f_1 \succ f_2 \succ f_3 \succ m_1$
m_2	$f_1 \succ f_2 \succ f_3 \succ m_2$
m_3	$f_2 \succ f_1 \succ m_3 \succ f_3$
m_4	$f_2 \succ f_3 \succ f_1 \succ m_4$

Female	Preference
f_1	$m_4 \succ m_1 \succ m_2 \succ m_3 \succ f_1$
f_2	$m_2 \succ m_1 \succ m_3 \succ m_4 \succ f_2$
f_3	$m_3 \succ m_1 \succ m_2 \succ m_4 \succ f_3$



Example: Coalition Game

- What coalitions will be formed?
- How to distribute profits to coalition members to make the coalition stable?

	{P ₁ }	{P ₂ }	{P ₃ }	{P ₁ , P ₂ }	{P ₁ , P ₃ }	{P ₂ , P ₃ }	{P ₁ , P ₂ , P ₃ }
profit	2	6	12	9	15	21	24

- Suppose $(x_1, x_2, x_3) = (5, 6, 13)$
- Can $\{P_1, P_2\}$ block (x_1, x_2, x_3) ?
- Can $\{P_2, P_3\}$ block (x_1, x_2, x_3) ?
- What are the results if $(x_1, x_2, x_3) = (3, 7, 14)$?

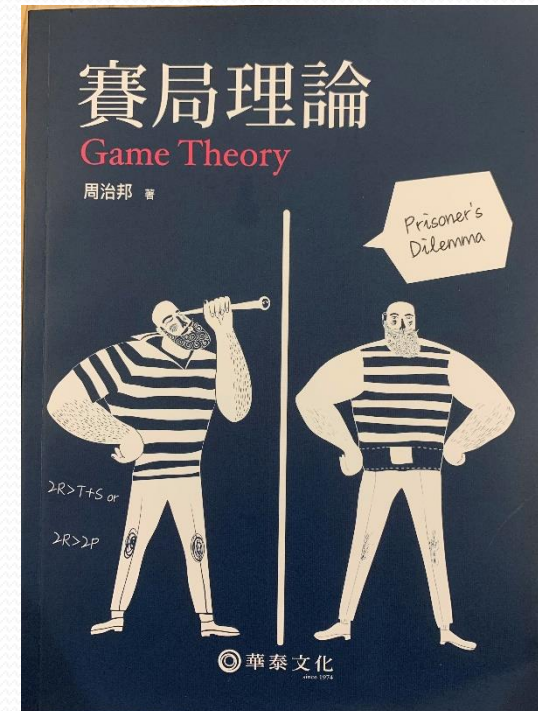
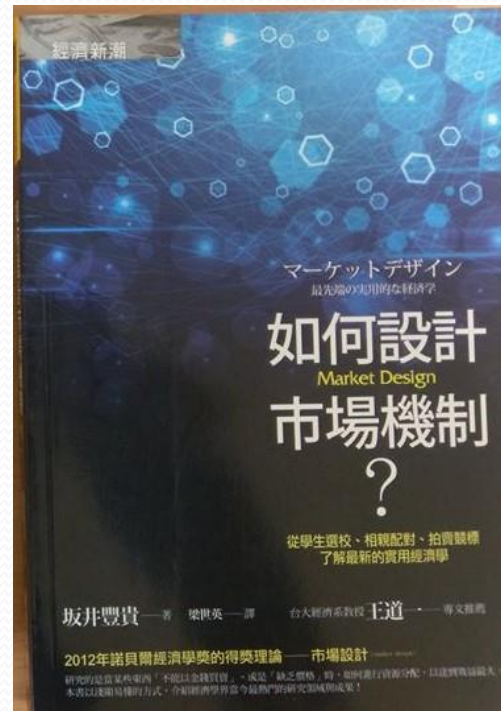
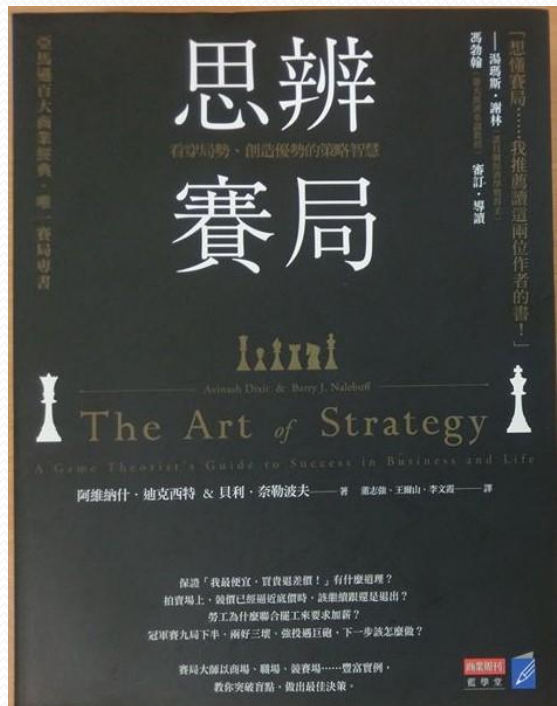
Course Goal Four: Help Us Solve

- **Compute strategies for players** to stabilize or improve the game
 - perhaps without full knowledge of the game
- Reinforcement learning can help
- New materials since this year



Text Book: None

- Reference books (in Chinese)



Schedule (tentative)

week	contents	week	contents
1	Introduction and non-cooperative games	9	Matching Theory (1/2)
2	Non-cooperative games (cont.)	10	Matching Theory (2/2)
3	Some Useful Non-Cooperative Games	11	Auctions
4	Game Designs for Network Problems (1/2)	12	Coalition Game (1/2)
5	Game Designs for Network Problems (2/2)	13	Coalition Game (2/2)
6	Game Designs for Graph Problems	14	Report & presentation (1)
7	Learning for non-cooperative games	15	Report & presentation (2)
8	Review and Mid-term Exam.	16	Final Exam.

Scoring Policy

- (60+%) Quizzes + Assignments
 - 4 quizzes
 - 2 programs
- (20%) Mid-term exam.
- (20%) Final report

Course Materials

- All lectures will be recorded and put online
- Slides are placed in E3 Learning Management System:
<https://e3.nycu.edu.tw/my/>
- Because all announcements are sent via E3, please confirm your e-mail address setting in E3 is correct
- Instructor's e-mail: lhyen@nctu.edu.tw (lhyen@nycu.edu.tw someday)